

Announcements

- HW 3 is due this Saturday
- HW 4 will be out this Saturday, but will only have 1 problem
- Project presentation in two weeks
 - Will post schedule soon; let me know if you prefer to present first or last.

CMSC 3540I: The Interplay of Economics and ML (Winter 2024)

Learning From Strategic Data Sources

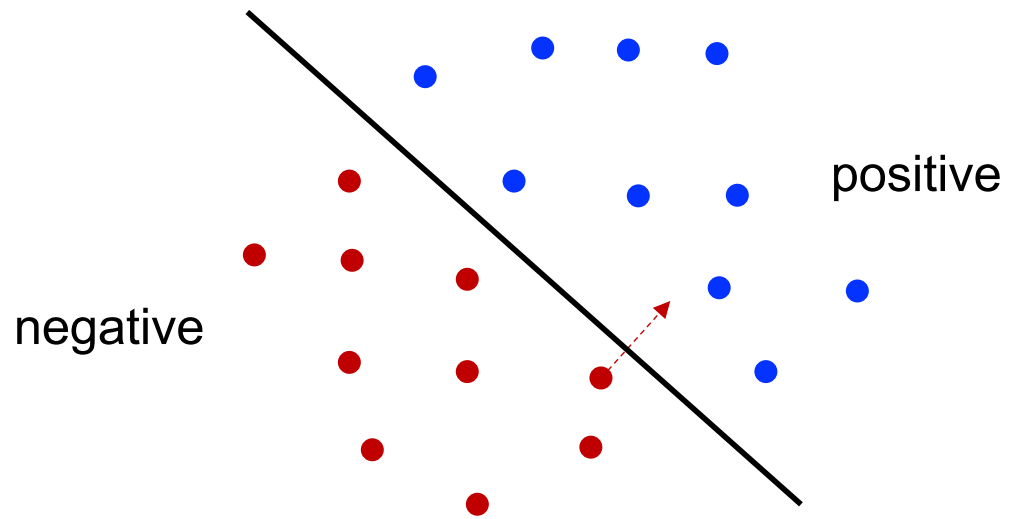
Instructor: Haifeng Xu



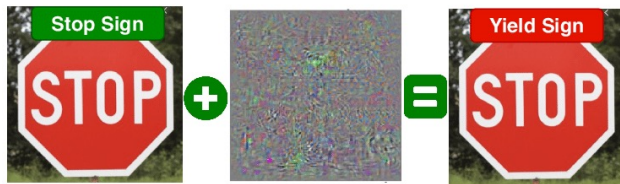
Outline

- Introduction to Strategic Classification
- Learnability and Computability of Strategic Classifiers
- Beyond Classification

Classification



Data points' features may be manipulated



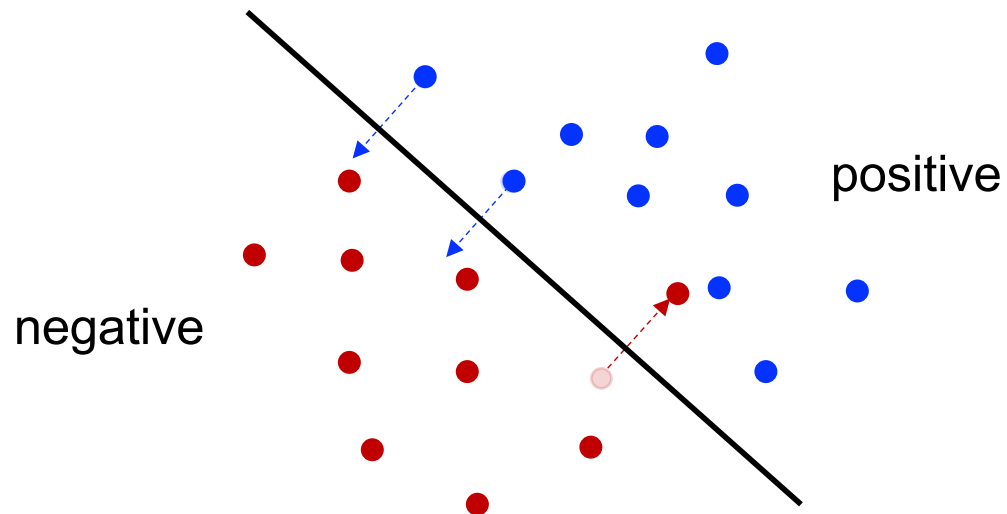
Adversarial attack

[Goodfellow et al.'15]

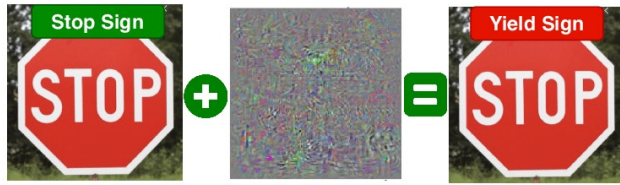
[Eykholt et al.'18]

[Cullina et al.'18]

.....



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Adversarial attack



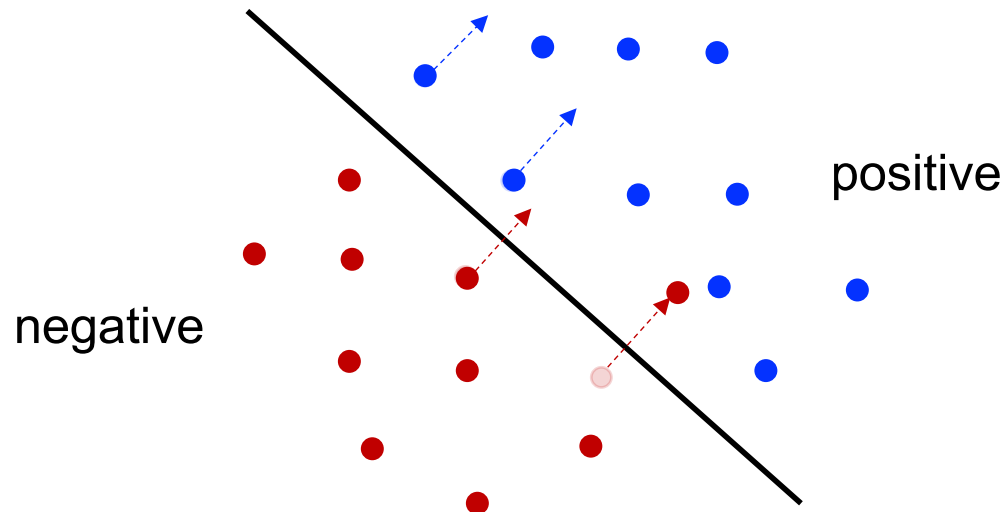
Strategic manipulation

[Hardt et al.'16]

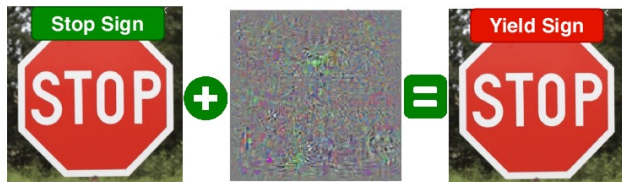
[Hu et al.'19]

[Ghalme et al.'21]

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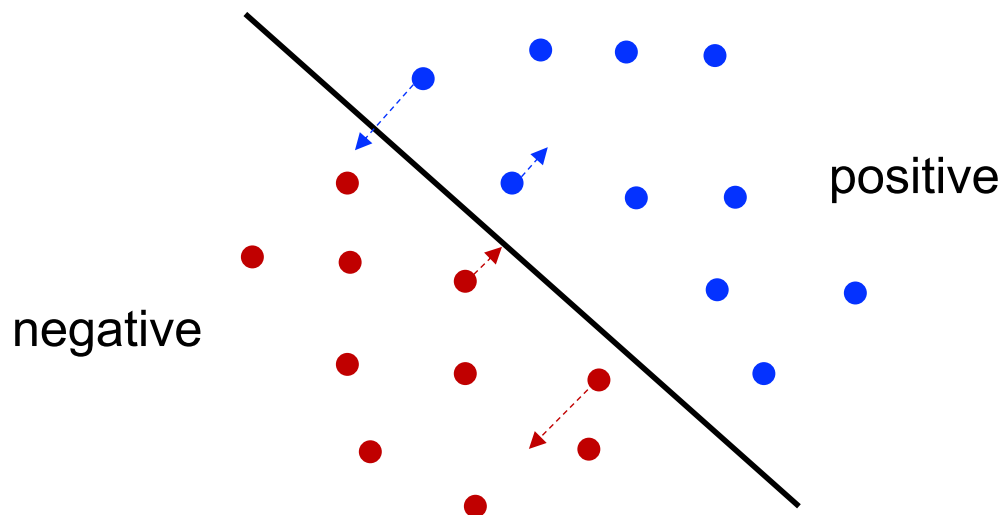
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Adversarial attack



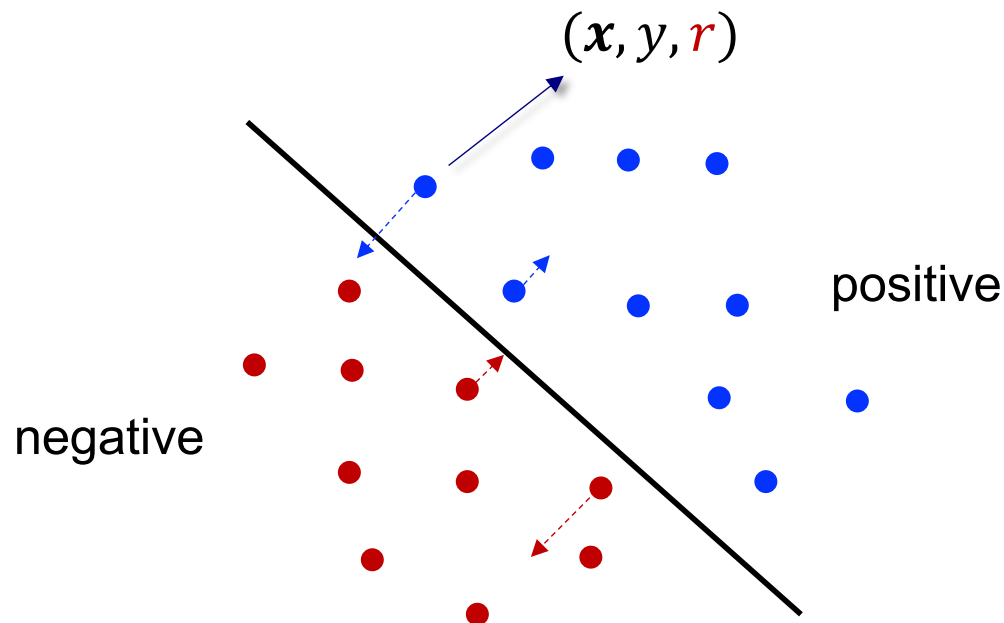
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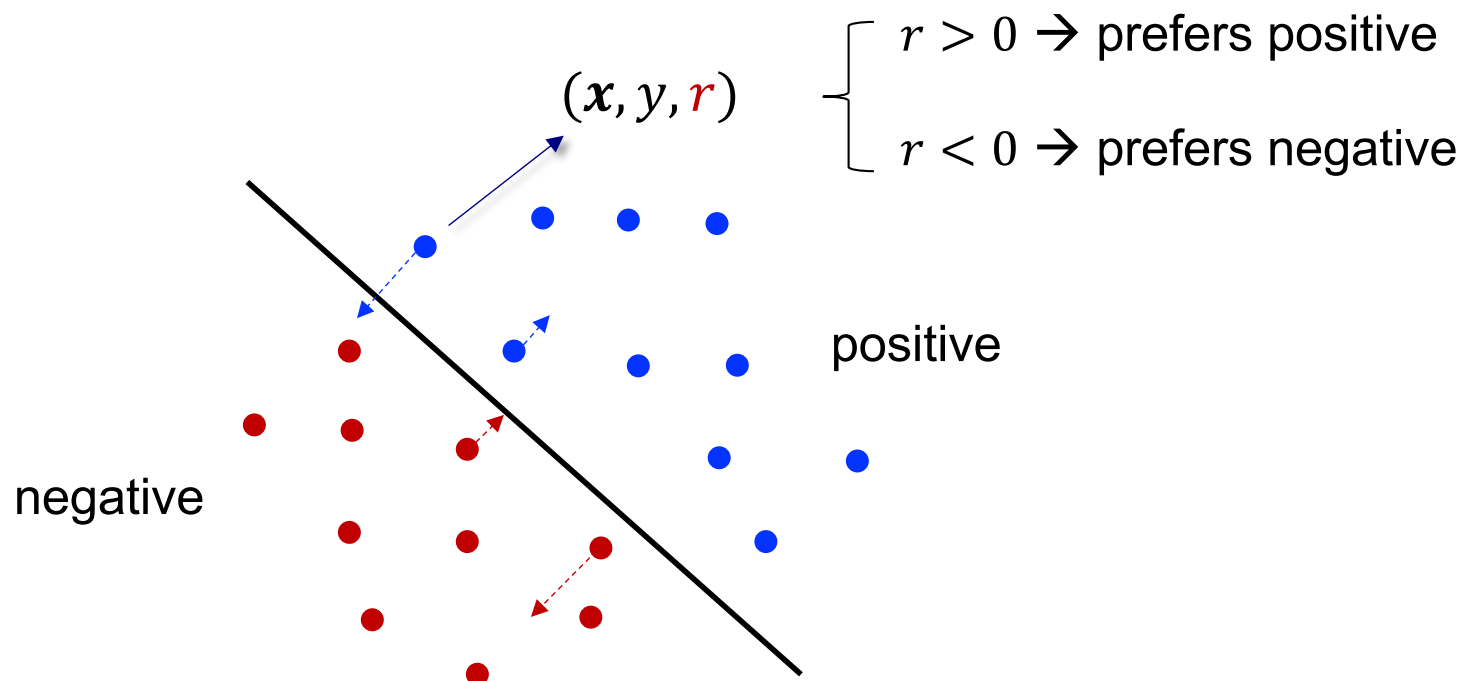
A Unified Model of Strategic Classification

- Each data point is an individual agent, represented by (x, y, r)
 - $r \in \mathbb{R}$ capture the point's incentive of being classified as positive



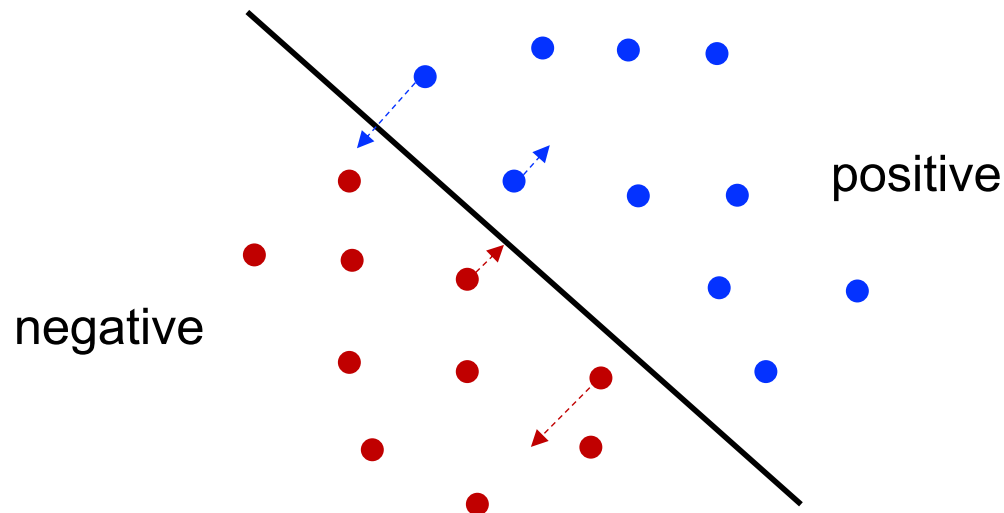
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 - c is an arbitrary semi-norm
- Given classifier $f: X \rightarrow \{0, 1\}$, data point (x, y, r) will manipulate its feature to z that maximizes utility

$$\underbrace{r \cdot \mathbb{I}(f(\mathbf{z}) = 1)}_{\text{reward from classification outcome}} - \underbrace{c(\mathbf{x} - \mathbf{z})}_{\text{Manipulation cost}}$$

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- Given classifier $f: X \rightarrow \{0, 1\}$, data point (x, y, r) will manipulate its feature to

$$z^*(x, r; f) = \arg \max_{z \in X} [r \cdot \mathbb{I}(f(z) = 1) - c(x - z)]$$

This is a game now!

A Unified Model of Strategic Classification

The Strategic Classification Problem

Input: n uncontaminated training data $(\mathbf{x}_1, y_1, r_1), \dots, (\mathbf{x}_n, y_n, r_n) \sim \mathcal{D}$

Learning goal: compute a classifier f that predicts well based only on the manipulated feature $\mathbf{z}^*(\mathbf{x}, r; f)$

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Some notably special cases

- ✓ $r \equiv 0 \rightarrow$ classic classification
- ✓ $r \equiv 1 \rightarrow$ strategic classification (cf. [Hardt et al.'16])
- ✓ $r = -y \rightarrow$ adversarial classification (cf. [Cullina et al.'18])
- ✓ $\text{sgn}(r) = -y \rightarrow$ generalized adversarial classification

Remark: manipulation here does not change true label

Strategic Classifications are Everywhere

➤ University admissions

- Students academic records are selectively revealed
- **Heterogeneous preferences: not all students prefer the same school**

The screenshot shows the top section of the University World News website. At the top is the logo 'University World News' with the tagline 'THE GLOBAL WINDOW ON HIGHER EDUCATION' and a blue circular logo with 'UW' inside. Below the logo is a navigation bar with links: 'Global Edition', 'Africa Edition', 'Asia Hub', 'Transformative Leadership', 'Special Reports', and 'Events'. A purple banner on the left reads 'MA in Higher Education Management' with the subtitle 'A unique programme for higher education leaders'. To the right of this is a white banner with the text 'Apply now for May 2020' and the logo of the University of Bath School of Management. Below these banners is a news article section. On the left, there are social media links: 'Join us on Facebook' and 'Follow us on Twitter'. The main article is titled 'How will artificial intelligence change admissions?' by Marguerite J Dennis, dated 26 October 2018. It has a 'GLOBAL' tag and a red bookmark icon. Below the article title are social sharing buttons for LinkedIn (Share), Twitter (Tweet), and Facebook (Share 13).

Strategic Classifications are Everywhere

- University admissions
 - Students academic records are selectively revealed
- Classify loan lending decisions
 - Borrowers will selectively report their features
 - **Heterogeneous preferences: not all borrowers prefer the same loan**



30-Year
Fixed

v.S

15-Year
Fixed

Strategic Classifications are Everywhere

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- We decide which restaurants to go based on Yelp rating
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- Hiring job candidates in various scenarios

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- Hiring job candidates in various scenarios
- Note: this problem deserves study even you do classification manually instead of using an automated classifier

Manipulation in Stock Trading

Spoofing is the practice of submitting large **spurious** buy (sell) orders to create artificial demand (supply) and mislead other traders.

UBS, Deutsche Bank and HSBC to pay millions in spoofing settlement, CFTC says

- Deutsche Bank will pay \$30 million, UBS \$15 million and HSBC \$1.6 million to settle civil charges that some of their traders engaged in spoofing in the precious metals market.
- The CFTC charged six individuals, and the Department of Justice charged eight with crimes related to deceptive trading in a wide-ranging investigation.

Liz Moyer

Published 2:29 PM ET Mon, 29 Jan 2018 | Updated 8:32 AM ET Wed, 31 Jan 2018



Luke MacGregor | Reuters

Flash Crash Trader E-Mails Show Spoofing Strategy, U.S. Says

by Tom Schoenberg, Suzi Ring, Janan Hanna
@TSchoenberg22 @journosoz

September 3, 2015 – 4:03 PM EDT Updated on September 4, 2015 – 9:32 AM EDT



Navinder Singh Sarao leaves Westminster Magistrates' Court in London, on Friday, Aug. 28, 2015. Photographer: Chris Ratcliffe/Bloomberg

- ▶ Failed orders are 'costing me,' Sarao said to tell programmer
- ▶ Indictment's new details seen bolstering U.S. extradition case

US seals first prosecution against stock market trader for 'spoofing'

A jury convicts Michael Coscia on six charges of commodities fraud and six charges of spoofing, all of the charges he faced

9 0 4 13 Email



Prosecutors said Michael Coscia wanted to lure other traders to markets by creating an illusion of demand so that he could make money on smaller trades Photo: AP

By Reuters

11:48PM GMT 03 Nov 2015

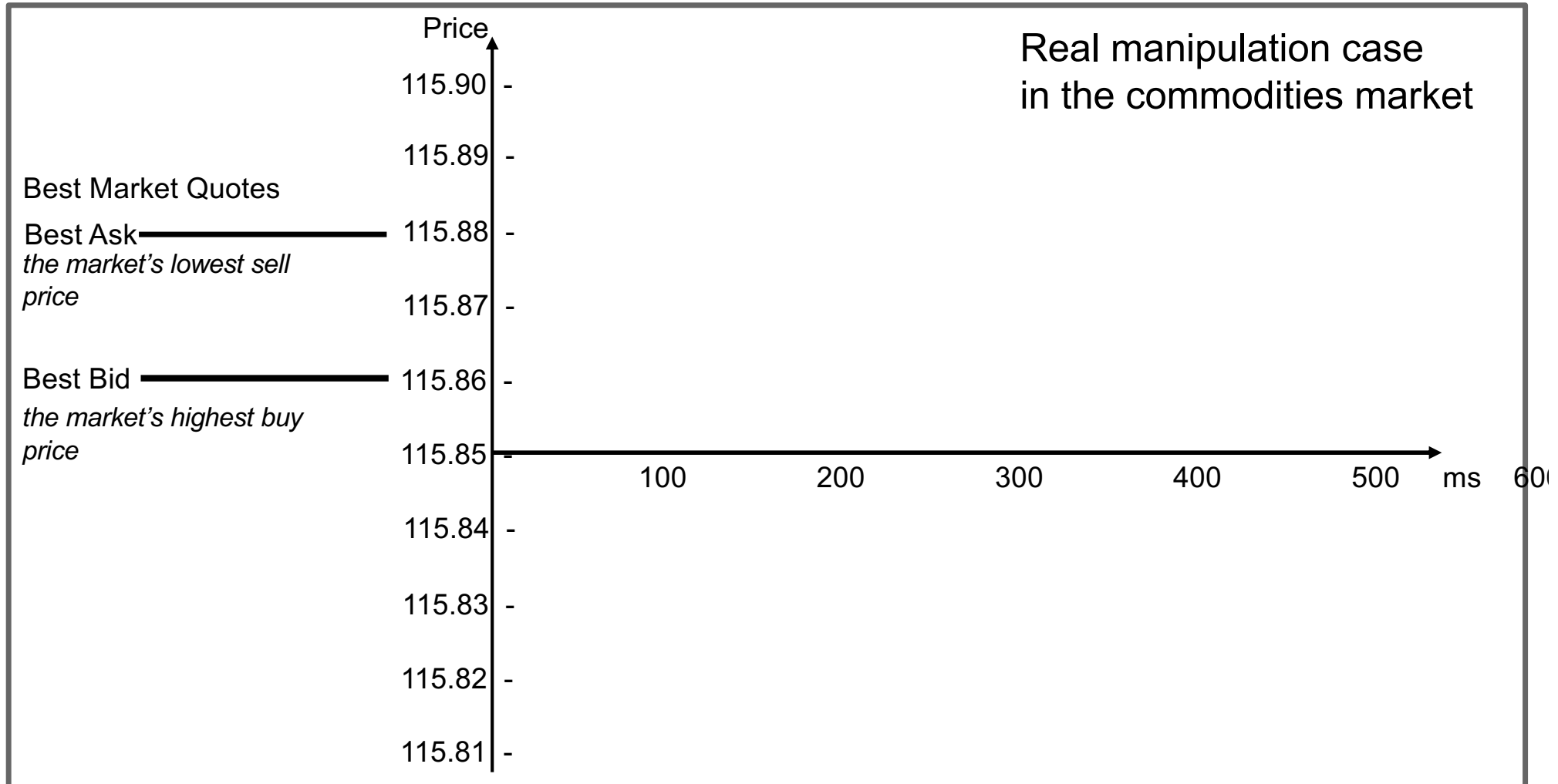
A US jury has found high-frequency trader Michael Coscia guilty of commodities fraud and "spoofing" in the US government's first criminal

Useful sources

<https://www.fca.org.uk/publication/final-notices/coscia.pdf>

<https://www.fca.org.uk/publication/final-notices/coscia-appendix-1a.pdf>

Manipulation in Stock Trading



Source: Financial Conduct Authority, Animated Example of Mr. Coscia's Trading

Manipulation in Stock Trading



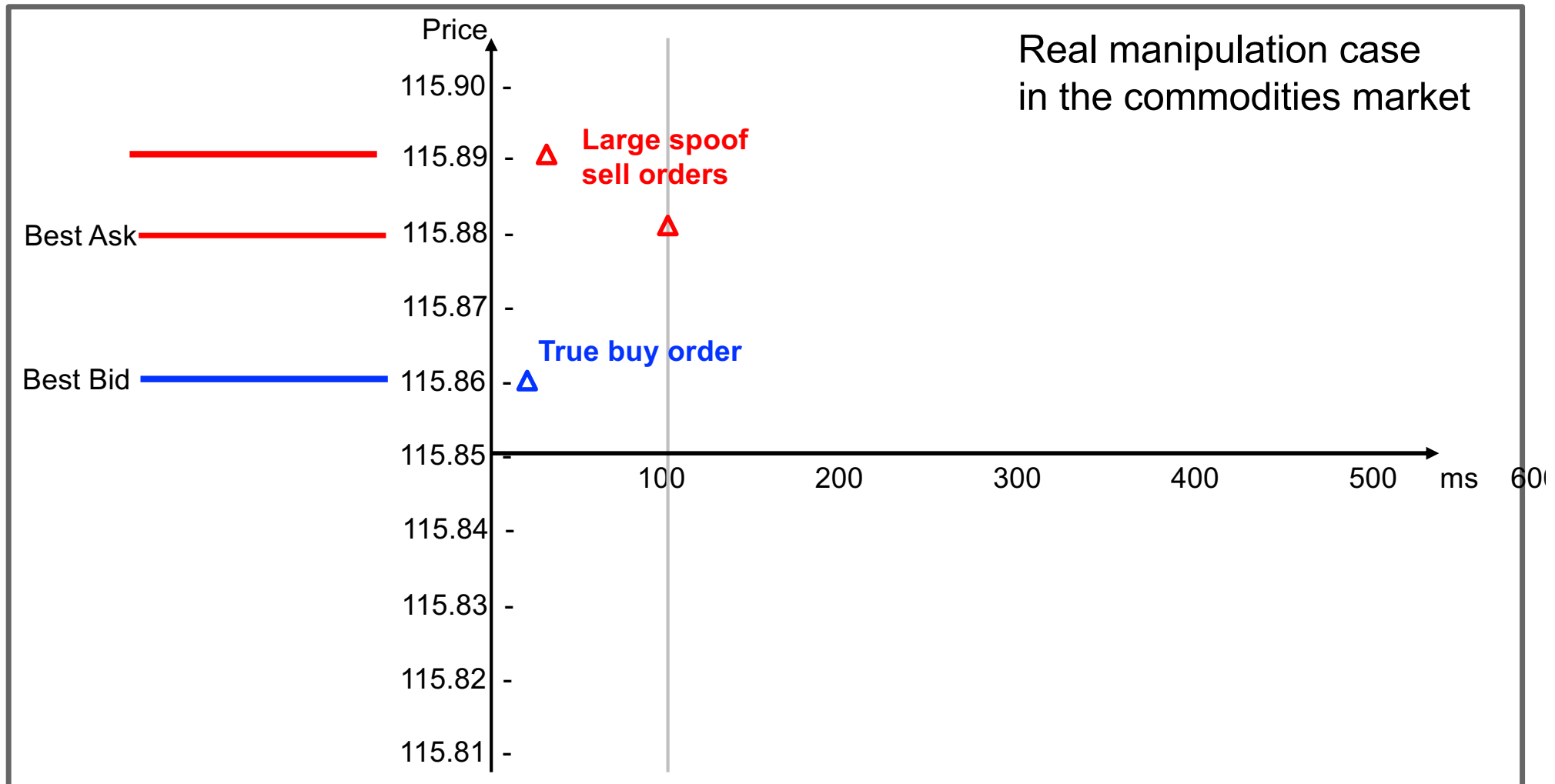
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Manipulation in Stock Trading



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Recall...

The Strategic Classification Problem

Input: n uncontaminated training data $(x_1, y_1, r_1), \dots, (x_n, y_n, r_n) \sim \mathcal{D}$

Learning goal: compute a classifier f that predicts well based only on the manipulated feature $z^*(x, r; f)$

But will this general problem still be learnable? 

In classic ML setup

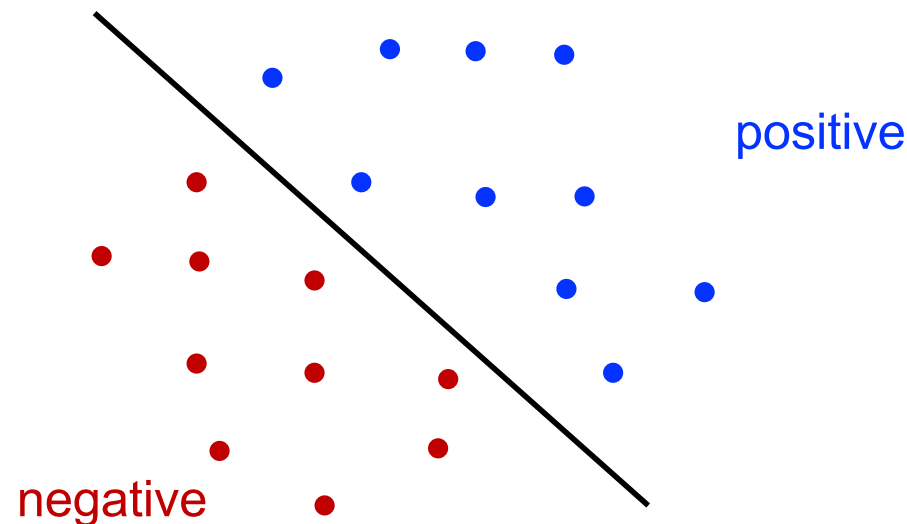
- ✓ Learnability (sample complexity) of a hypothesis class is governed by its **VC-dimension**
- ✓ The learning algorithm is the **empirical risk minimization** (ERM)

The Learnability of Strategic Classifiers

... is governed by a variant, coined **strategic VC-dimension (SVC)**

The Learnability of Strategic Classifiers

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- Defined over the **equilibrium** of the classification outcome



Challenge is to characterize the classification outcomes under strategic manipulation

The Learnability of Strategic Classifiers

... is governed by a variant, coined **strategic VC-dimension (SVC)**

Theorem. Any strategic classification instance is (PAC) learnable via a **strategic variant of ERM**, with sample complexity

$$n(\epsilon, \delta) = \Theta\left(\frac{SVC + \log(1/\delta)}{\epsilon^2}\right)$$

where ϵ is accuracy loss and δ is the failure probability.

Unifies learnability of all previous special cases

- Generalizes the fundamental theorem of classic PAC learning ($r = 0$)
- Recovers the main sample complexity result of [Hardt et al.'16] with $r = 1$, for which we show their $SVC = 3$
- Generalizes learnability of adversarial classification [Cullina et al.'18] with $r = -y$

The Learnability of Strategic Classifiers

... is governed by a variant, coined **strategic VC-dimension (SVC)**

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$$n(\epsilon, \delta) = \Theta\left(\frac{SVC + \log(1/\delta)}{\epsilon^2}\right)$$

where ϵ is accuracy loss and δ is the failure probability.

Implies learnability of many new setups with heterogeneous data preferences: loan approval, student admission, classifying job candidates,...

Strategic Empirical Risk Minimization

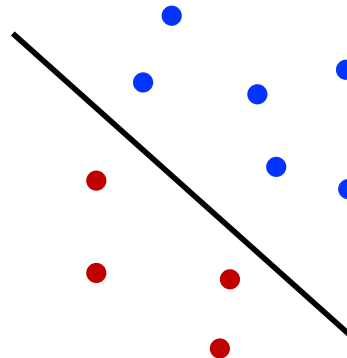
Input: n uncontaminated training data $(\mathbf{x}_1, y_1, r_1), \dots, (\mathbf{x}_n, y_n, r_n) \sim \mathcal{D}$

Output: a classifier $h(\mathbf{z})$ that minimizes “strategic risk”

$$\text{SERM: } \min_h \sum_{i=1}^n \mathbb{I}[h(\mathbf{z}_i) \neq y_i]$$

$$\text{s. t. } \mathbf{z}_i = \arg \max_{\mathbf{z} \in X} [r_i \cdot \mathbb{I}(h(\mathbf{z}) = 1) - c(\mathbf{x}_i - \mathbf{z}_i)], \forall i$$

- Strategic ERM minimizes empirical risk by accounting for manipulation



Strategic Empirical Risk Minimization

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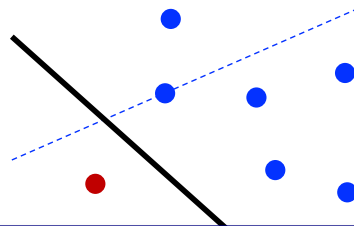
$$\text{s. t. } \mathbf{z}_i = \arg \max_{\mathbf{z} \in X} [r_i \cdot \mathbb{I}(h(\mathbf{z}) = 1) - c(\mathbf{x}_i - \mathbf{z}_i)], \forall i$$

- Strategic ERM minimizes empirical risk by accounting for manipulation
- This is a bi-level optimization problem (a Stackelberg game with n followers)
 - Difficult to solve due to non-smooth objective functions

Instantiation to Linear Classification

Theorem. The SVC of d -dimensional linear classifiers is at most $d + 1$.

- $d + 1$ is the VC of linear classifiers in classic setup
- Learning strategic linear classifiers is **no harder statistically**
- Why can SVC be smaller than VC dimension?



Lessons Learned

Flexibility of manipulating features reduces the “richness” of possible classification outcomes, and may make it easier to learn

Computing Strategic Linear Classifier

Unfortunately, not all news is good...

Theorem. Strategic empirical risk minimization (ERM) is NP-hard for linear classification.

Computing Strategic Linear Classifier

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Theorem. Strategic empirical risk minimization (ERM) is NP-hard for linear classification. But, strategic ERM can be solved in polynomial time when the instance is *essentially adversarial*.

$$\min^- = \min\{r : (\mathbf{x}, y, r) \text{ with } y = -1\} \text{ and}$$

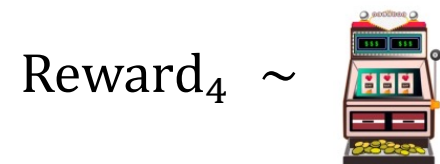
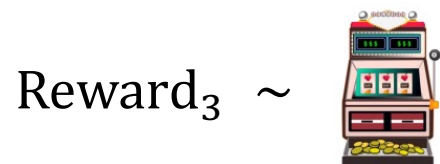
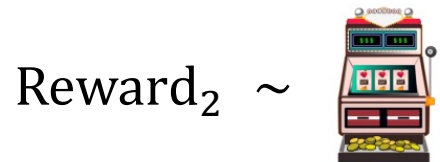
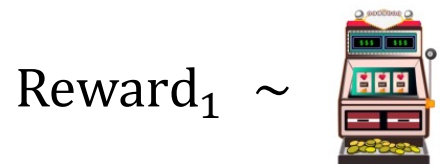
$$\max^+ = \max\{r : (\mathbf{x}, y, r) \text{ with } y = +1\}$$

Essentially adversarial if $\min^- \geq \max^+$

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Vignette I: Manipulation in Multi-Armed Bandits



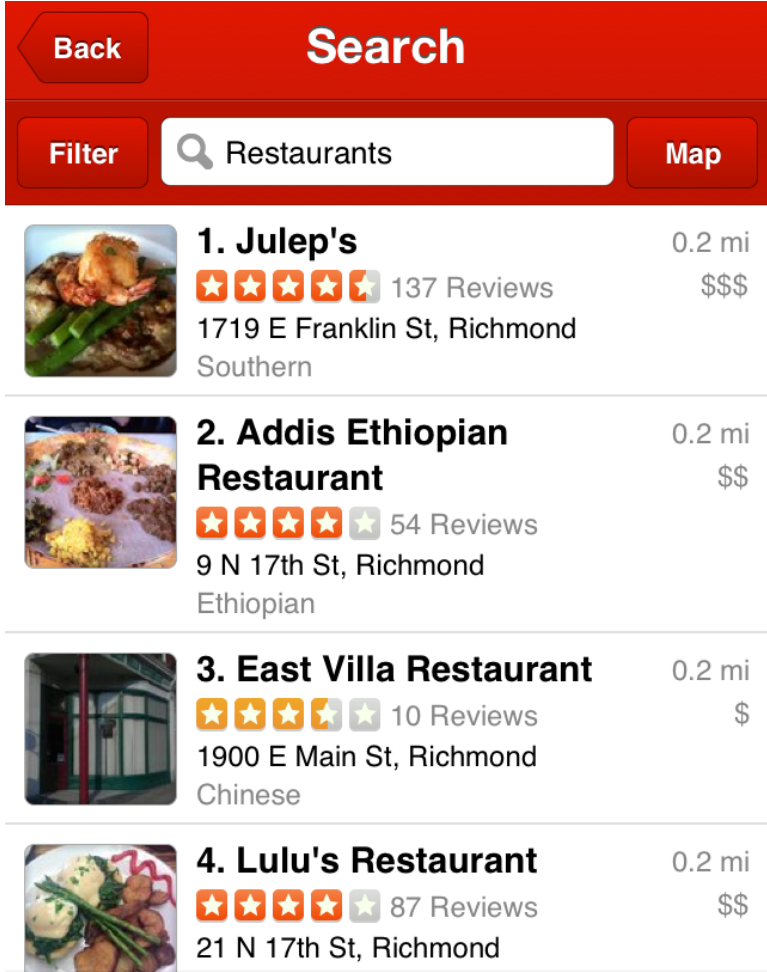
Vignette I: Manipulation in Multi-Armed Bandits

Reward₁ ~

Reward₂ ~

Reward₃ ~

Reward₄ ~



The screenshot shows a mobile application interface for searching restaurants. At the top is a red header with a 'Back' button and the word 'Search'. Below the header is a search bar containing the text 'Restaurants', flanked by 'Filter' and 'Map' buttons. The search results are listed in a table-like format with four entries:

Rank	Restaurant Name	Distance	Price	Reviews	Address	Cuisine
1.	Julep's	0.2 mi	\$\$\$	137 Reviews	1719 E Franklin St, Richmond	Southern
2.	Addis Ethiopian Restaurant	0.2 mi	\$\$	54 Reviews	9 N 17th St, Richmond	Ethiopian
3.	East Villa Restaurant	0.2 mi	\$	10 Reviews	1900 E Main St, Richmond	Chinese
4.	Lulu's Restaurant	0.2 mi	\$\$	87 Reviews	21 N 17th St, Richmond	

Each arm has incentives to manipulate its rewards to induce more pulls

Vignette I: Manipulation in Multi-Armed Bandits

Theorem. Most standard stochastic bandit algorithms (including UCB, ϵ -Greedy and Thomas Sampling) are all robust to selfish arms' strategic reward manipulation.

- A sharp contrast to adversarial reward attacks, which can ruin all these algorithms easily

Vignette 2: Distinguish Distributions from Strategic Samples



The Trouble of Professor Bob

Vignette 2: Distinguish Distributions from Strategic Samples



Current postdoc Charlie is happy . . .

Vignette 2: Distinguish Distributions from Strategic Samples



They know what each other is thinking...

Vignette 2: Distinguish Distributions from Strategic Samples

- A **distribution** $l \in \{g, b\}$ arrives, which can be a good distribution (g) or a bad one (b)
- An **agent** has access to n i.i.d. samples from l , from which he chooses a **subset of exactly m samples** as his report
 - Agent's goal: persuade a **principal** to accept l
- Principal observes agent's report, and decides whether to accept
 - Principal's goal: accept when $l = g$ and reject when $l = b$
 - Want to minimize her **probability of mistakes**

Other applications: e.g., deciding where to hold Olympics based on photographs of different city locations



vs



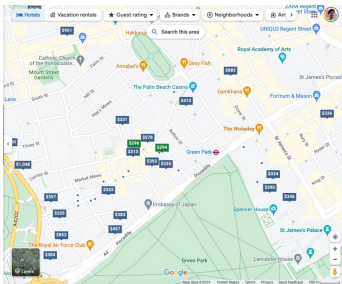
vs



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VS



VS



Concluding Remarks

- Very active research area, with motivations from numerous economic applications
- Strategic studies of classification (online or offline, training time vs testing time), regression, bandits, reinforcement learning...
 - Closely related to adversarial attack and algorithm robustness as well
- This lecture – manipulation does not change true nature
 - Next lecture – “[strategic improvement](#)”

Thank You

Haifeng Xu

University of Chicago

haifengxu@uchicago.edu