CMSC 35401:The Interplay of Economics and ML (Winter 2024)

The Economics of Online Content Creation and Generative Als

Instructor: Haifeng Xu



Online Content Creation is a Huge Economy





Meta Net Ad Revenues Worldwide, by Segment, 2020-2024

billions





In this section I will define briefly how we can derive the back propagation algorithm. Here I only list the key steps in the derivation ...

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dlvu.github.id



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backpropagation with rigorous formulation

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CMU School of Computer Science http://www.cs.cmu.edu > Werbos.backprop.pdf PDF

Backpropagation through time

by PJ WERBOS \cdot Cited by 6665 — Under certain conditions, this can be a **rigorous** approac but its generality is limited, and it requires great care with the side conditions (which are rarel 11 pages

Oeep Learning @ VU

https://dlvu.github.io > slides > dlvu.lecture02.pdf PDF

Lecture 2: Backpropagation - Peter Bloem

Today's lecture will be entirely devoted to the **backpropagation** algorithm. The heart of all de learning. part 1: review part 2: scalar **backpropagation** part 3 ... 46 pages

ScienceDirect.com

https://www.sciencedirect.com > topics > computer-science

Backpropagation Algorithm - an overview

The **backpropagation** algorithm performs learning on a multilayer feed-forward neural network it iteratively learns a set of weights for prediction of the class ...

Medium · zfeng 1 like · 3 years ago

Coding back propagation algorithm from scratch | by zfeng

In this section I will define briefly how we can derive the **back propagation** algorithm. Here I only list the key steps in the derivation ...



ChatGPT 4 ~

You

Could you use explain backpropagation to me with rigorous formulations?

ChatGPT

Certainly! To explain backpropagation with a more rigorous formulation, we'll delve into the mathematics that underpin the algorithm. This involves understanding how the gradient of the loss function is computed with respect to the weights of the network and how these gradients are used to update the weights in a way that minimizes the loss.

Notation and Setup

Let's consider a simple feedforward neural network with L layers, where each layer l has $n^{[l]}$ neurons. The network takes an input x and produces an output \hat{y} , aiming to approximate the true output y. Each layer l has a weight matrix $W^{[l]}$, a bias vector $b^{[l]}$, and an activation function $g^{[l]}$.

Forward Pass

[1]

[1] / [1]

- 1. Input Layer: The input layer receives the input $x = a^{[0]}$.
- 2. Hidden Layers and Output Layer: For each layer l from 1 to L, the pre-activation value $z^{[l]}$ and the activation $a^{[l]}$ are putted as follows: • $z^{[l]} = W^{[l]}a^{[l-1]} + b^{[l]}$

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🔿 Meta



Labeling Al-Generated Images on Facebook, Instagram and Threads

Shop v Our technologies v About us v Build with us v

February 6, 2024 By Nick Clegg, President, Global Affairs







Getty Images sues AI art generator Stable Diffusion in the US for copyright infringement



The competition not only affects the Internet ecosystem, but also has real-world consequences







This is the critical time to rethink online content ecosystem and how generative AIs (GenAIs) will affect/reshape it



1. GenAls as representations of an Internet content ecosystem



2. GenAls create part of an Internet content ecosystem





1. GenAls as representations of an Internet content ecosystem



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How would such GenAI technology affect content creation?



Google cut a deal with Reddit for Al training data



By Emma Roth, a news writer who covers the streaming wars, consumer tech, crypto, social media, and much more. Previously, she was a writer and editor at MUO. Feb 22, 2024, 10:24 AM PST

🕑 🥤 🍯 📔 20 Comments (20 New

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Reminder of This Lecture

...will zoom into the second mode

1. GenAls as representations of an Internet content ecosystem



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Reminder of This Lecture

...will zoom into the second mode

GenAls as representations of an Internet content eco

- Tries to answer one economic questions how AI content generation affects incentives of human creators in recommender systems and the equilibrium?
- Link to a relevant recent workshop at AAAI 2024











Credit: DALL.E

Texts

Human vs. Generative AI in Content Creation Competition: Symbiosis or Conflict?

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Paper link: https://arxiv.org/pdf/2402.15467.pdf







- i's user traffic from content topic k
- Captures competition (i.e., Tullock contest)





Similar studies of competition among (only) human creators has been widely studied recently, and also been applied to real systems



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Next: integrate GenAI into the competition





- ✓ GenAl as a new way for content creation
- May affect creators in two different ways

Model I: Exclusive Human-vs-GenAl Competition

- A special creator has exclusive access to GenAI (e.g., OpenAI or early adopters)
- Capture early stage of GenAI (e.g. now)



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Model I: Exclusive Human-vs-GenAl Competition

 \succ The same model, except that the share of users attracted to creator *i* is now $\frac{x_{ik}}{\alpha \cdot (\sum_j x_{jk})^{\beta} + \sum_j x_{jk}}$ on topic k special GenAl creator Creator *i* 29.576 posts 39 796 post Entertainment begins ar more at ETonline.com. Create $\alpha \cdot (\sum_{j} x_{jk})^{\beta}$ create $x_{ik} \in \mathbb{R}_+$ amount of contents amount of contents Competition captures the for topic ktension between GenAl and human creators Topic 3 Topic 2 Topic 1 μ_3 μ_2 μ_1

Model II: Inclusive Human-vs-GenAI Competition

Here GenAl technology has become mature enough that it is an option to every creator



a low-cost option that creates $\alpha \cdot (\sum_j x_{jk})^{\beta}$ amount of contents

Creator *i* 29.576 posts 39 796 p tertainment begins ore at ETonline.com. create $x_{ik} \in \mathbb{R}_+$ amount of contents for topic kTopic 3 Topic 2 Topic 1 μ_3 μ_2 μ_1

This competition captures tradeoff between adopting GenAI and creating authentic contents Next:

Some initial insights we obtained via game-theoretic analysis

Will start from exclusive human-vs-GenAI competition



Q1: does a (pure) Nash equilibrium (x_1^*, \dots, x_n^*) always exist?



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- ≻ Fortunately, YES if $\beta \in [0,1]$ and c_i convex in fact, it's unique
 - This is a pleasant surprise, since equilibrium of Tullock contests is generally complex
- > The new $\alpha \cdot (\sum_{j} x_{jk})^{\beta}$ term does not show up in any classic study of Tullock contests
 - A unique feature of ML that depends on aggregated data



 β = scaling exponent

Q1: does a (pure) Nash equilibrium (x_1^*, \dots, x_n^*) always exist?

- >Key proof idea: it can be shown to be a monotone game
 - Side product: many natural no-regret learning dynamics converge to equilibrium
- >Moreover, this equilibrium provably admits natural properties:
 - More cost-efficient human creators generate more contents
 - More human creators lead to more total body of contents

Q2: Will GenAI drive humans out of the ecosystems? Are there still authentic contents at equilibrium and, if so, how much?

>A fortunately positive answer – they will reach certain "symbiosis"

Theorem [YLNW**X**'24]: Suppose cost function is *weighted* l_{ρ} -norm (i.e., $c_i(\mathbf{x}_i) = \sum_k c_{ik} (x_{ik})^{\rho}$), then at the unique pure NE we have

$$\frac{(s_k^*)^{\rho}}{u_k \left| \left| \boldsymbol{c}_{\cdot k}^{-1} \right| \right|_{\frac{1}{\rho - 1}}} = C(\alpha, \rho)$$

where $s_k^* = \sum_i x_{ik}^*$ is the total human-created content for topic k and $c_{k}^{-1} = (c_{1k}^{-1}, c_{2k}^{-1}, \dots, c_{nk}^{-1})$ captures human production efficiency.

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- > GenAl's learning rate β did not show up in the bound (though it did affect equilibrium existence)
- > Note $\alpha = 0$ degenerates to no GenAl case, so competition with GenAl will not drive human out, but reduce total creation by a constant factor
- > Further analysis shows that as human become more efficient (i.e., $\downarrow \rho$),
 - more contents will be created for niche topic (small μ_k)
 - less contents will be created for popular topic (large μ_k)

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Remarks.

- Empirical simulation reveals that similar insights hold for general cost functions
- > All above results generalize to the $\mu_k(s_k)$ cases



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Q1: does a (pure) Nash equilibrium always exist?

>Unfortunately, not always, but YES under certain conditions

- Existence requires "light competition" i.e., sufficiently good scaling exponent of GenAI and fast-growing user demand
- Generally, not unique

Q2: How many human creators will resort to GenAI for content creation, and who are they?

Theorem [YLNWX'24]: Assume l_{ρ} -norm costs and light competition, then there always exists a pure Nash equilibrium of following format: on each topic k, creation at equilibrium is $(x_{1,k}, x_{2,k}, \dots, x_{m,k}, \bot, \dots, \bot)$ where \bot = GenAI and $c_{1,k} \leq c_{2,k} \leq \dots c_{m,k} < c_{m+1,k} \dots \leq c_{n,k}$.

1 - R

Moreover,

$$\frac{m}{n} \leq C(\alpha, \beta, \rho) \cdot \frac{(\mu_k)^{\frac{1-\rho}{\rho}}}{n^{1-\frac{(1-\beta)(\rho-1)}{\rho}}}$$

Takeaways

- Unsurprisingly, less efficient creators will switch to GenAls
- Less fraction of creators generate authentic contents when (a) topic is niche (small μ_k); or (b) competitive environment (large n); or (c) better GenAl technology
- > When *n* is significantly larger than μ_k , everyone switches to GenAI

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Remarks

> These insights are also observed in simulations, for more general setups

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> All above results generalize to the $\mu_k(s_k)$ cases

Summary

- Game-theoretic analysis about the competition of GenAl and human for content creation in recommendation systems
- Two different modes of competition, depending on the stage of the AI technology
- Economic analysis shows encouraging symbiosis between human and GenAl
 - No significant harm on the macro-level, but does not rule out possibility that a single individual human can may do significantly worse



Many Many Open Directions



Credit: DALL.E

≻Copyright issue

- What if GenAI platforms have to pay creators for acquiring their authentic data for training GenAIs, and how to acquire such data?
- >What if GenAI platforms charge creators for generating contents?
- Authentic contents can now profit from serving Internet users AND serving GenAI platforms – how would this change the competition?



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- >What if GenAI platforms charge creators for generating contents?
- Authentic contents can now profit from serving Internet users AND serving GenAI platforms – how would this change the competition?
- >What about the "search engine + conversational engine" competition?



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End of Lecturing for CMSC 35401

Hope you enjoyed the topics!

Next: Your Show Time



Thank You

Questions? haifengxu@uchicago.edu