

The Dynamics and Economy of Recommender Systems

Haifeng Xu

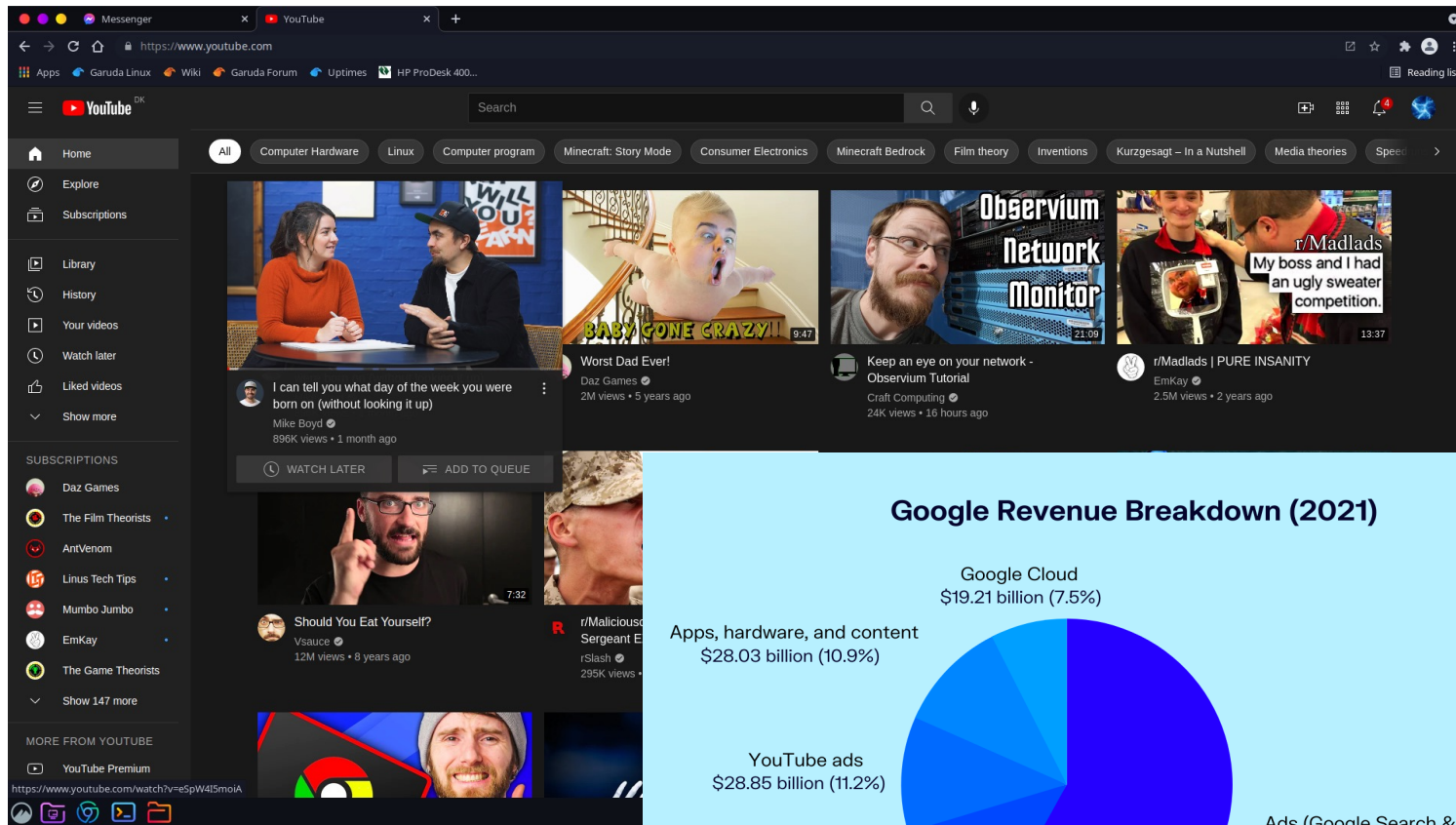
Department of Computer Science
and Data Science Institute

University of Chicago



Recommender System (RS)

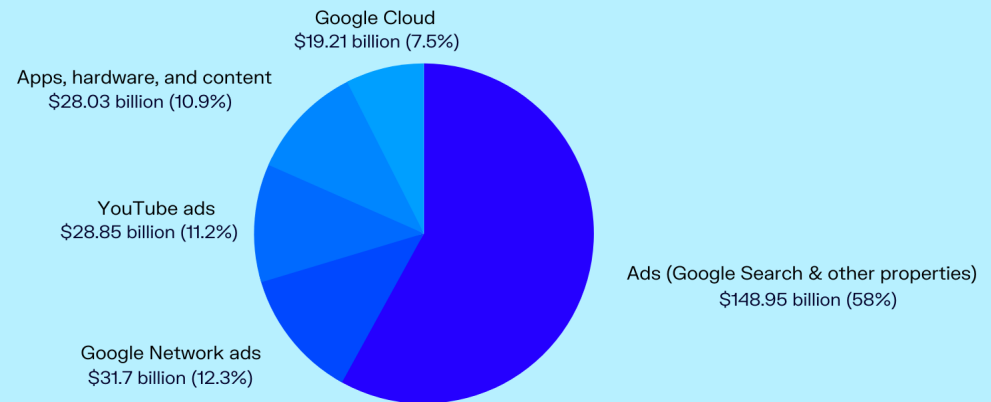
- An indispensable component of modern information systems



The screenshot shows a YouTube homepage with a grid of recommended videos. The videos include:

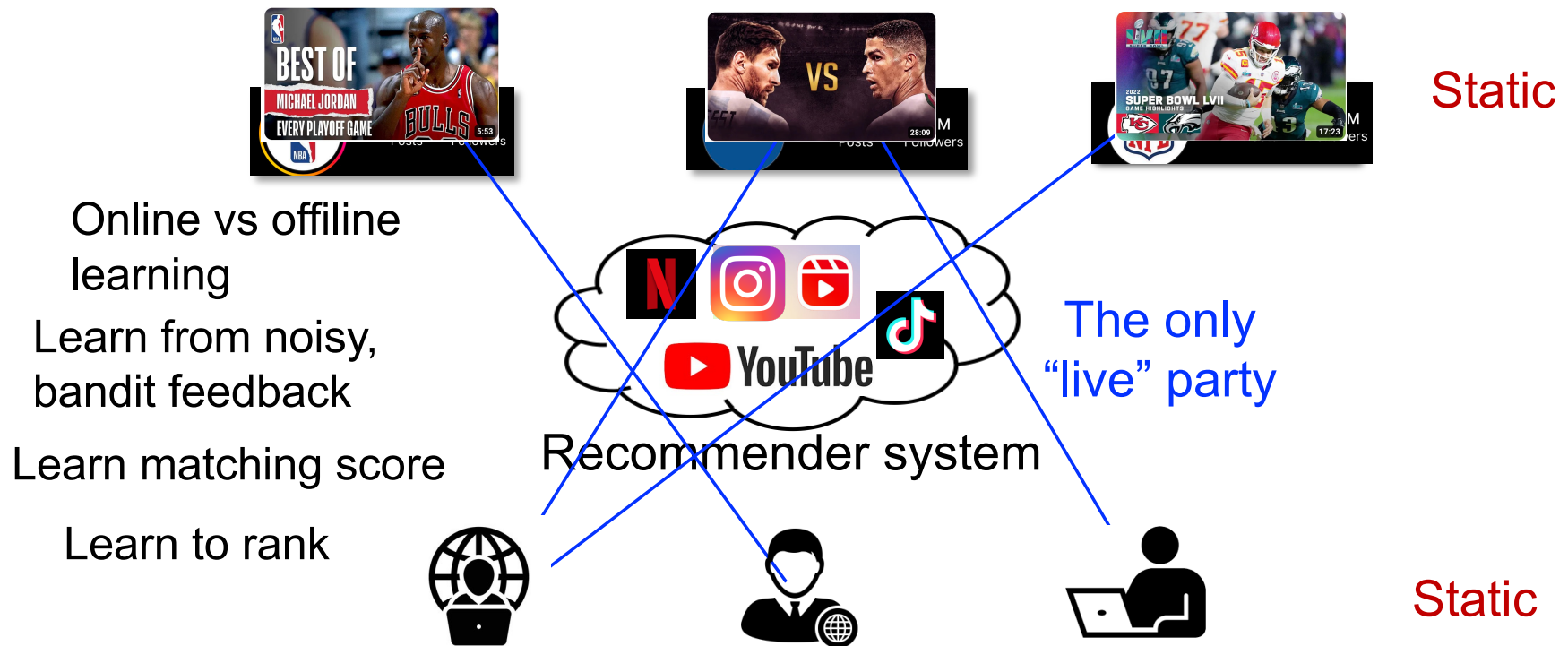
- "I can tell you what day of the week you were born on (without looking it up)" by Mike Boyd (896K views, 1 month ago)
- "Worst Dad Ever!" by Daz Games (2M views, 5 years ago)
- "Keep an eye on your network - Observium Tutorial" by Craft Computing (24K views, 16 hours ago)
- "r/Madlads | PURE INSANITY" by EmKay (2.5M views, 2 years ago)
- "Should You Eat Yourself?" by Vsauce (12M views, 8 years ago)
- "r/Malicious Sergeant E" by r/Slash (295K views)

Google Revenue Breakdown (2021)

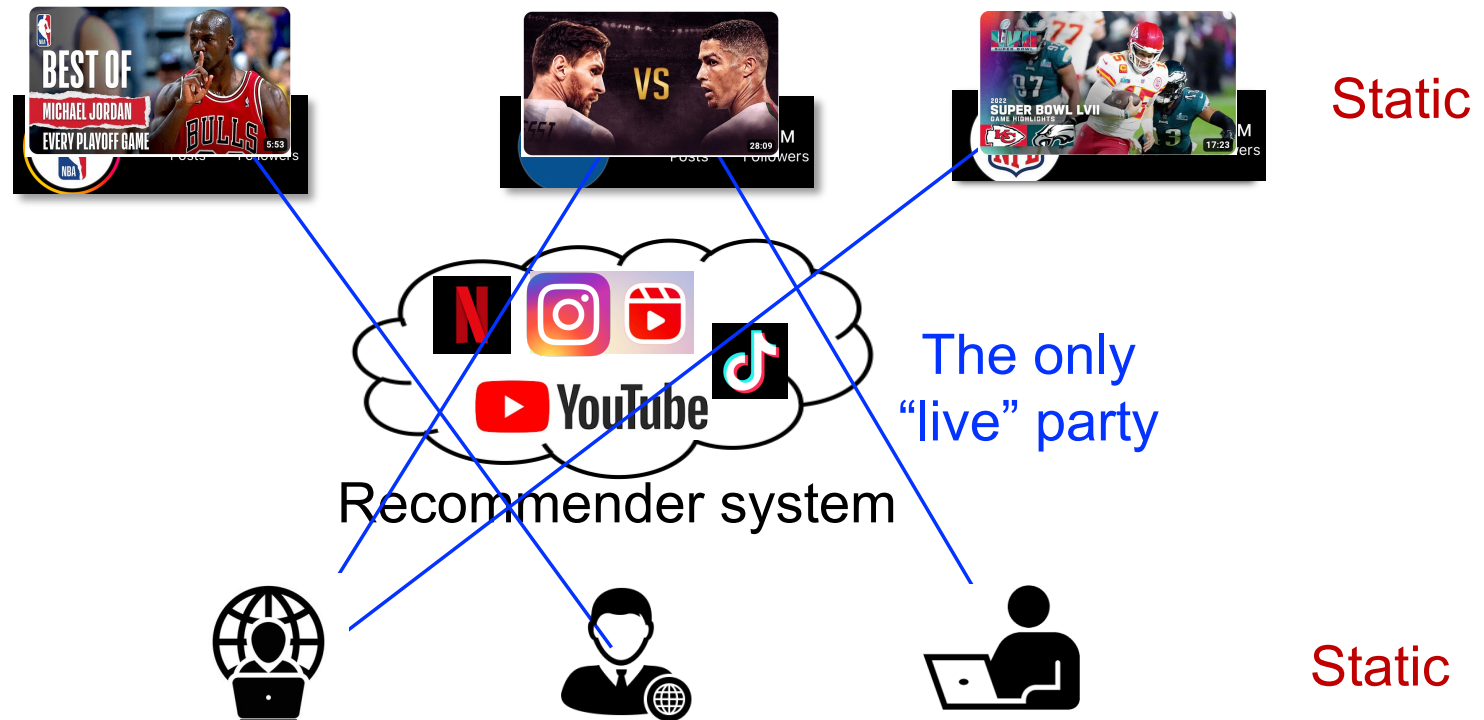


Classic Research Paradigm in RSs

System learning
in
static environments

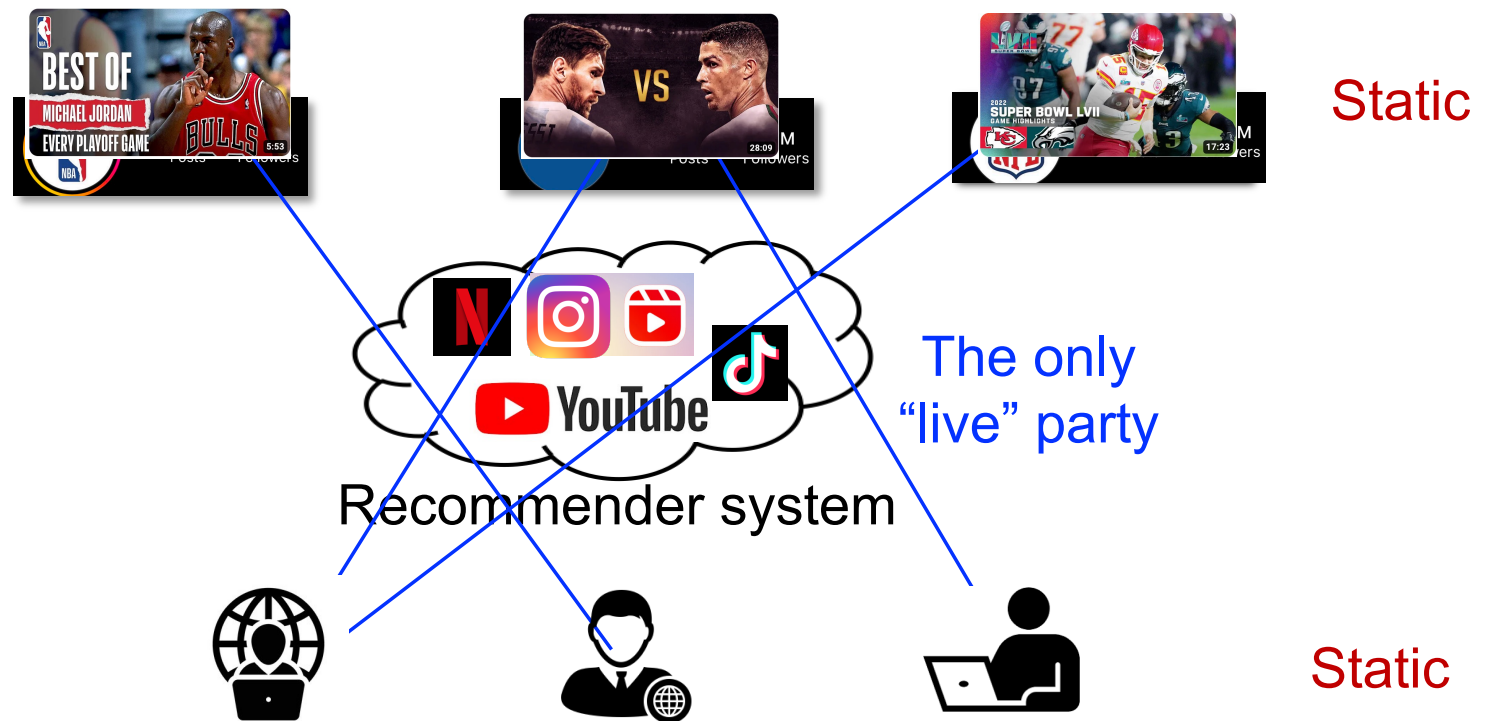


However...Numerous Evidence Supports Dynamic (Often Adaptive) Creator and User Behaviors



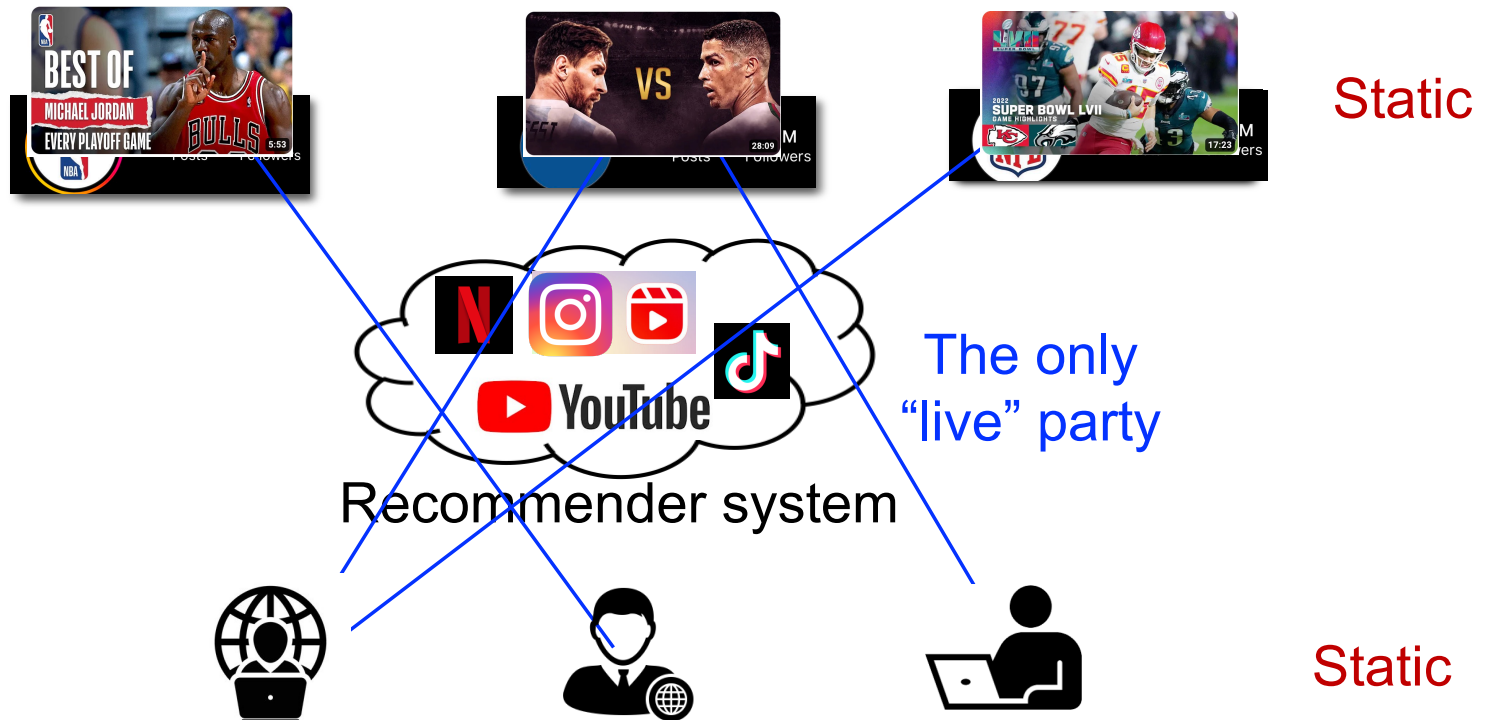
However...Numerous Evidence Supports Dynamic (Often Adaptive) Creator and User Behaviors

- **Creators** create longer videos after Youtube switches to use view duration to evaluate quality [MC'23]
- **RS users** are explorative at beginning (shown in many behavioral studies); Their feedback becomes more accurate only after sufficient experience



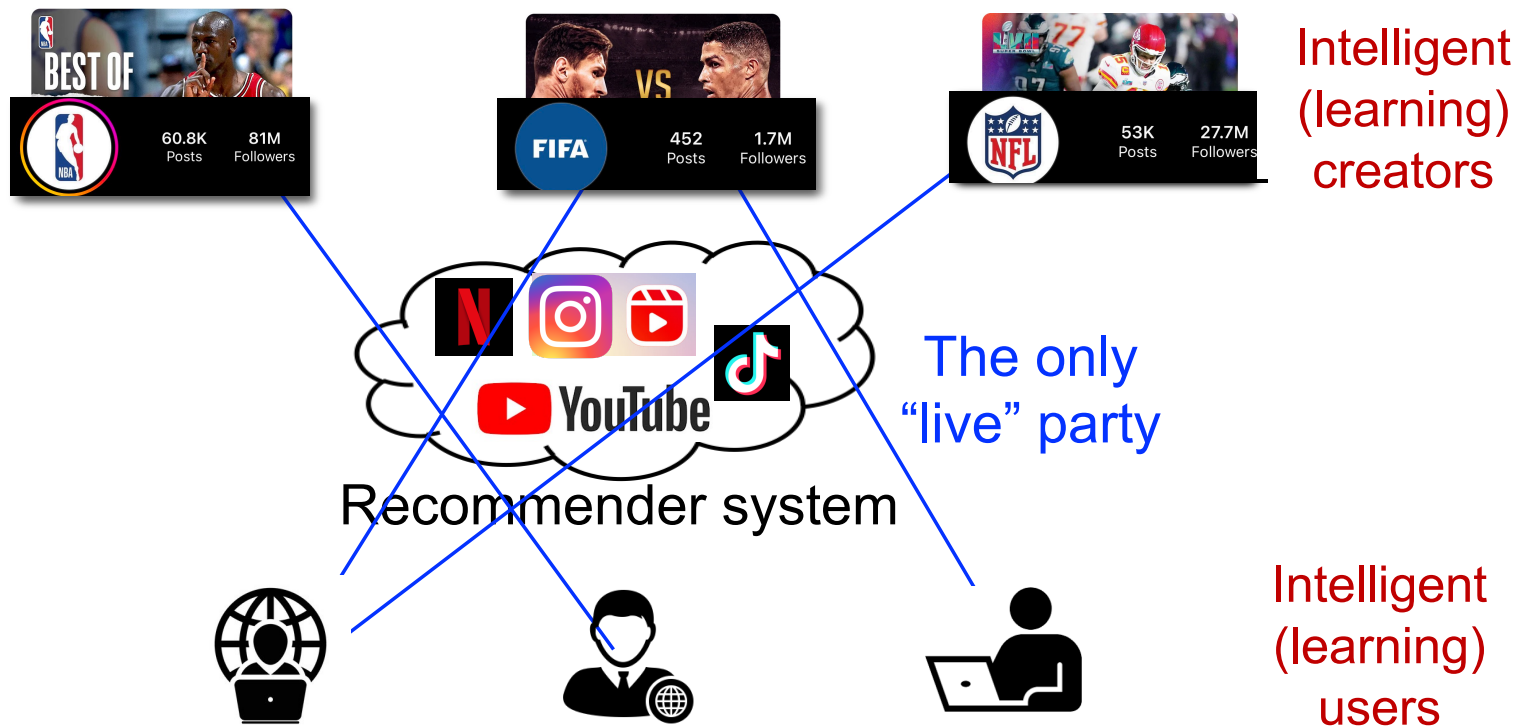
Rethinking this modeling paradigm....

System learning
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static environments



Rethinking this modeling paradigm....

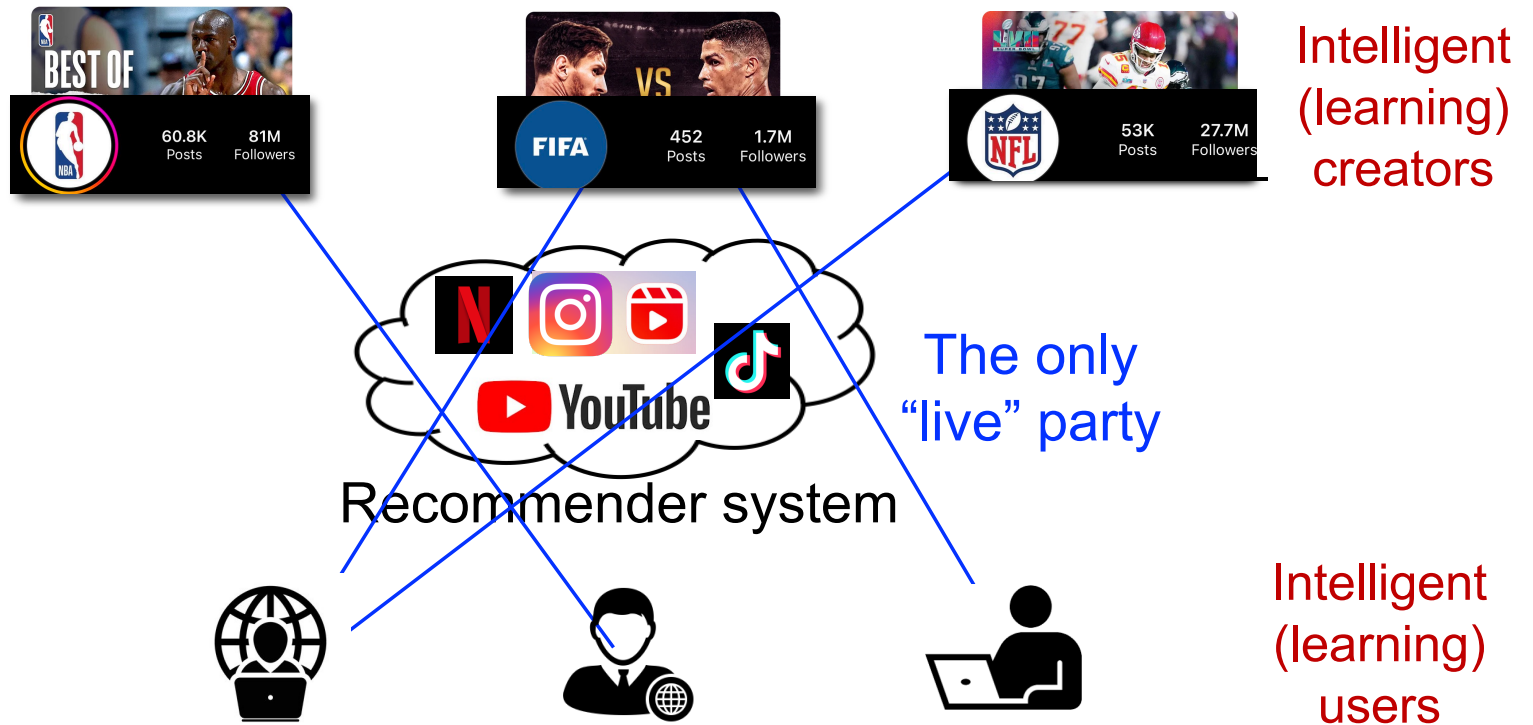
System learning
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Theme of This Talk

(multi-agent) economic modeling and optimization of recommender systems

Rethinking this modeling paradigm.... ~~Multi-agent~~ ~~System~~ learning in ~~non-stationary~~ ~~static~~ environments



Outline

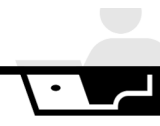


Intelligent

Part 1: Interacting with Strategic Creators

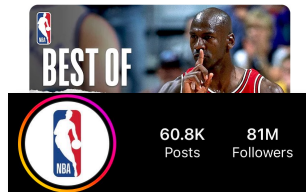


Part 2: Learning from Learning Users

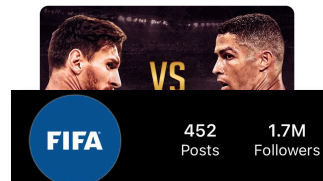


Intelligent
(learning)
users

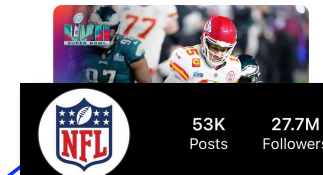
Utility maximizing
(learning) agent



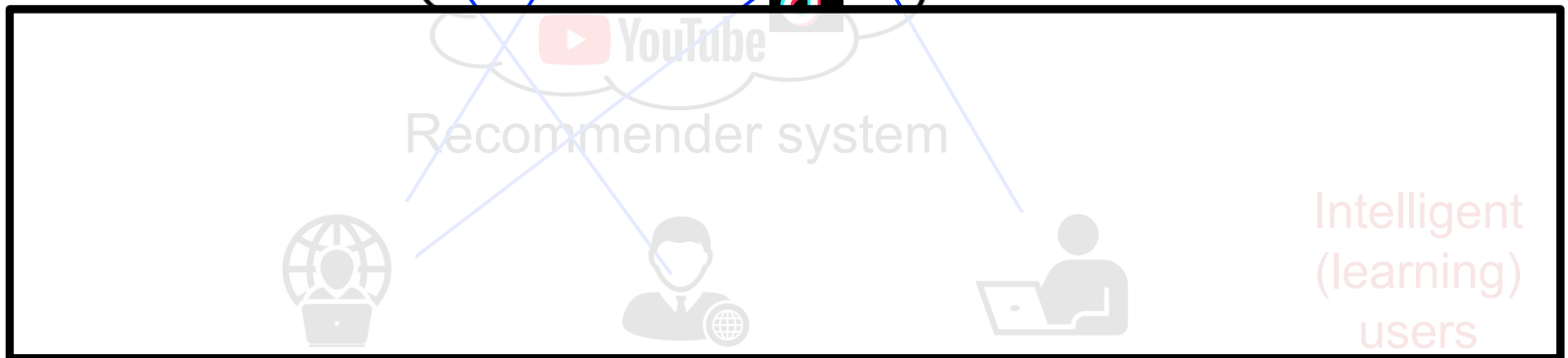
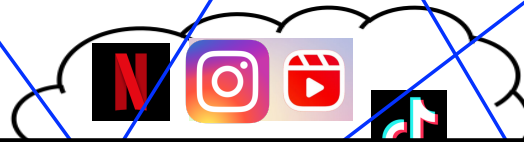
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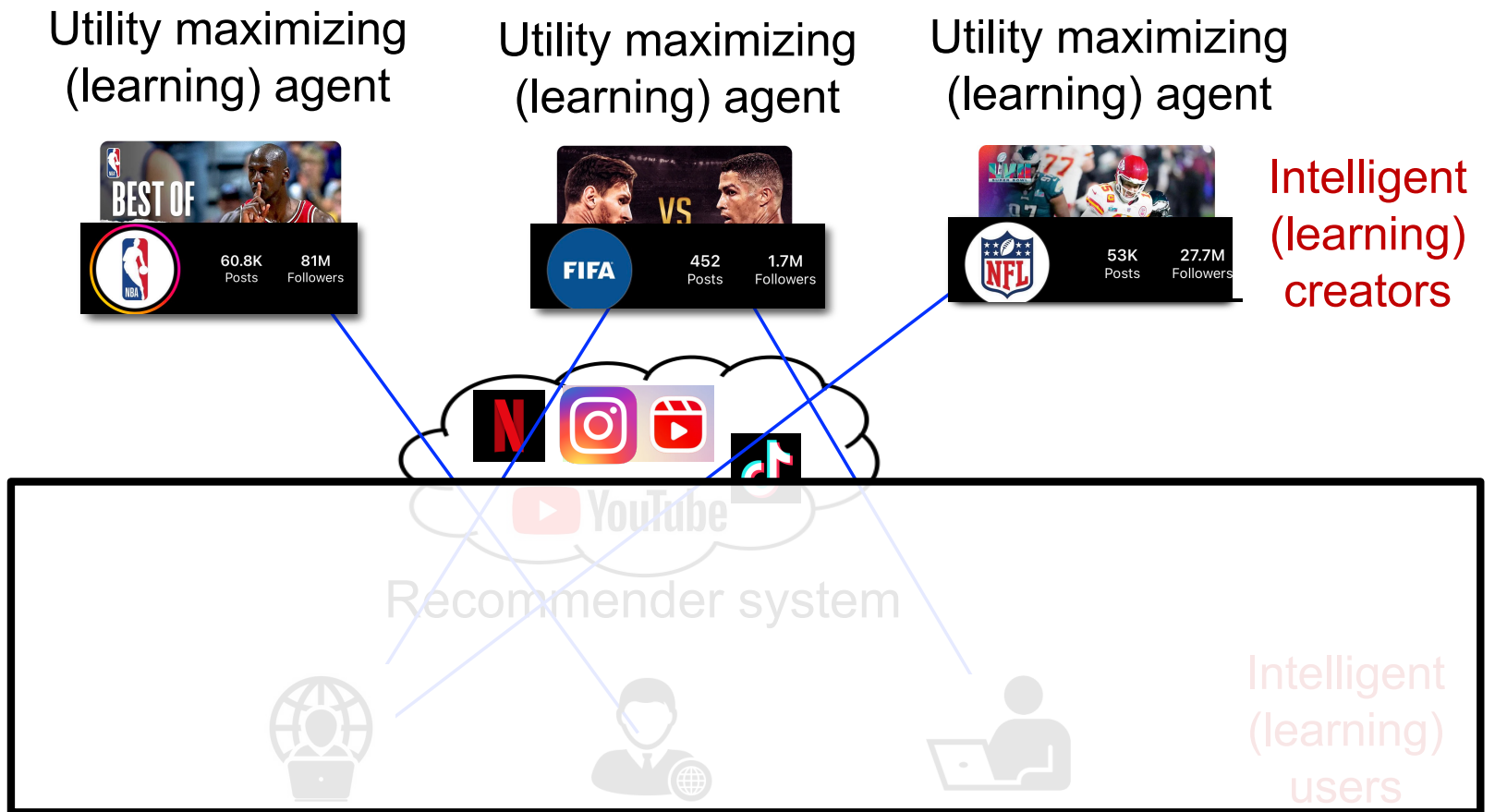
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Intelligent
(learning)
creators



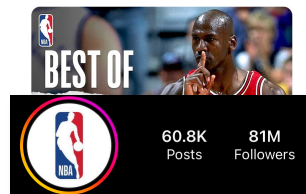
Q: do creators' learning dynamics converge to good or bad outcome?



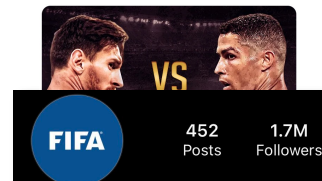
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The Competing Content Creation (C3) Game

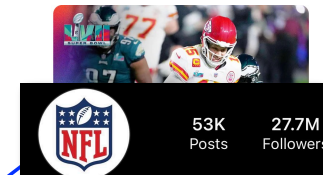
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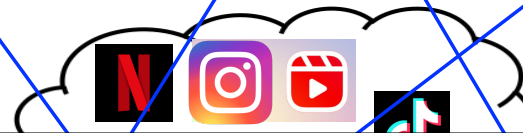
Utility maximizing
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Utility maximizing
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Intelligent
(learning)
creators



Reward Generating Environments

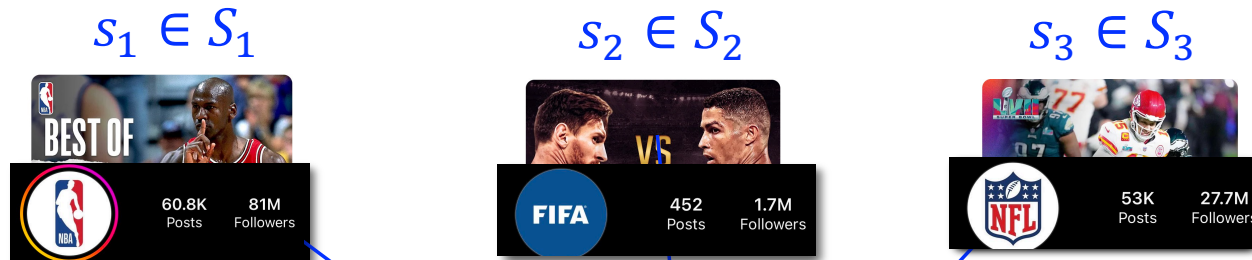


agent
(learning)
users

Q: do creators' learning dynamics converge to good or bad outcome?

The Competing Content Creation (C3) Game

Contents
(actions)



Estimated matching score: $\sigma(s_1, x)$ $\sigma(s_2, x)$ $\sigma(s_3, x)$

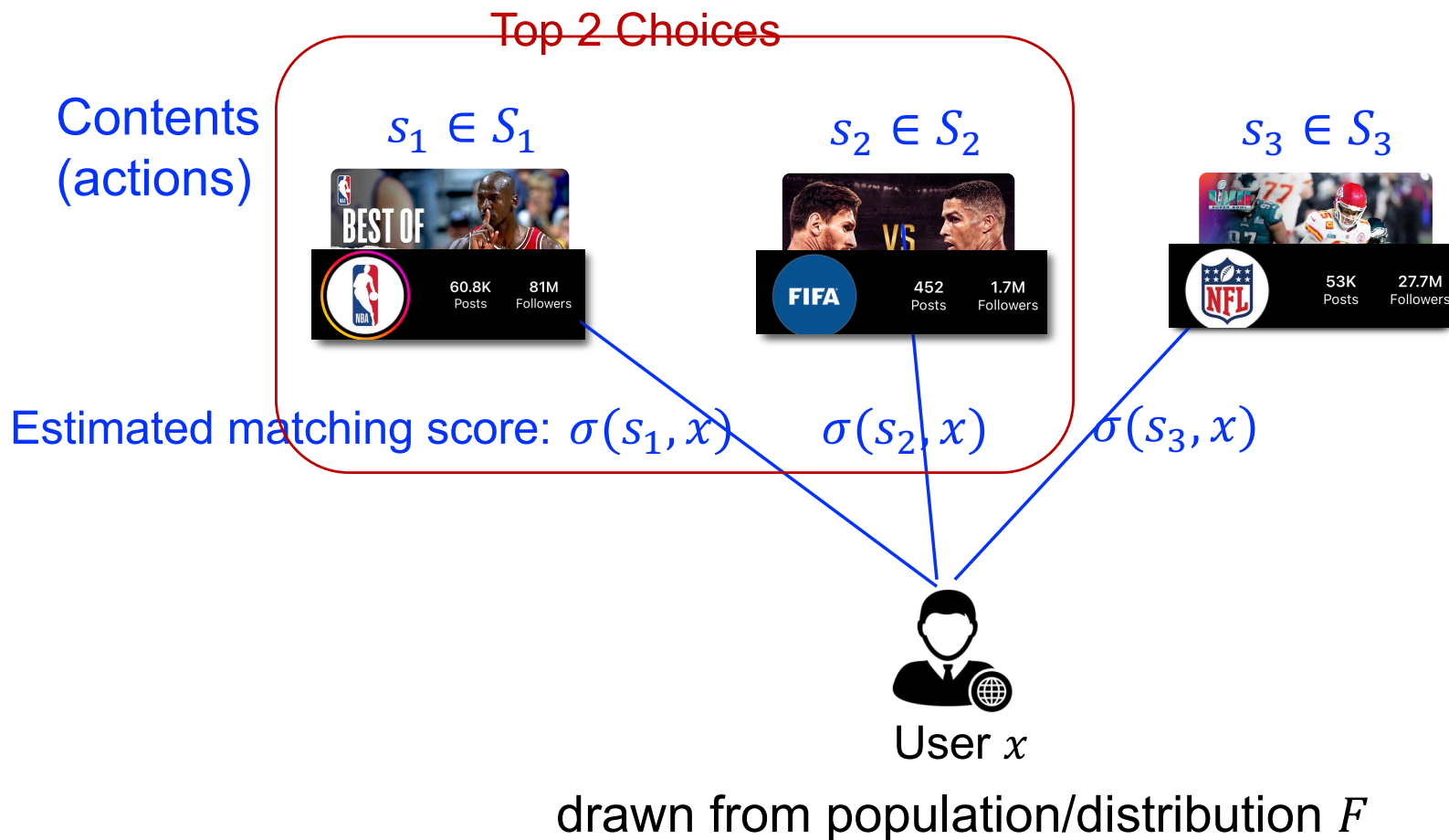


User x

drawn from population/distribution F

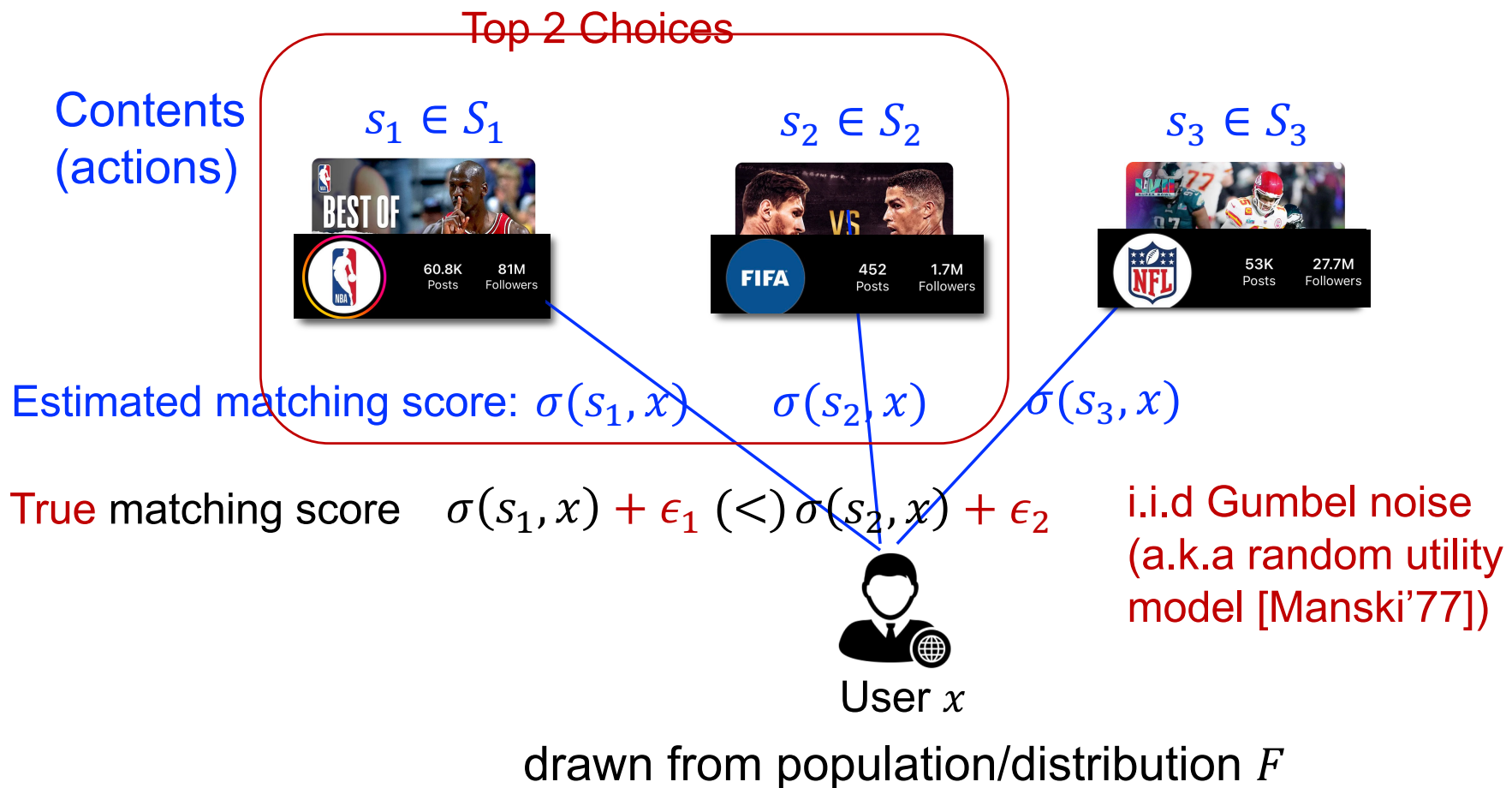
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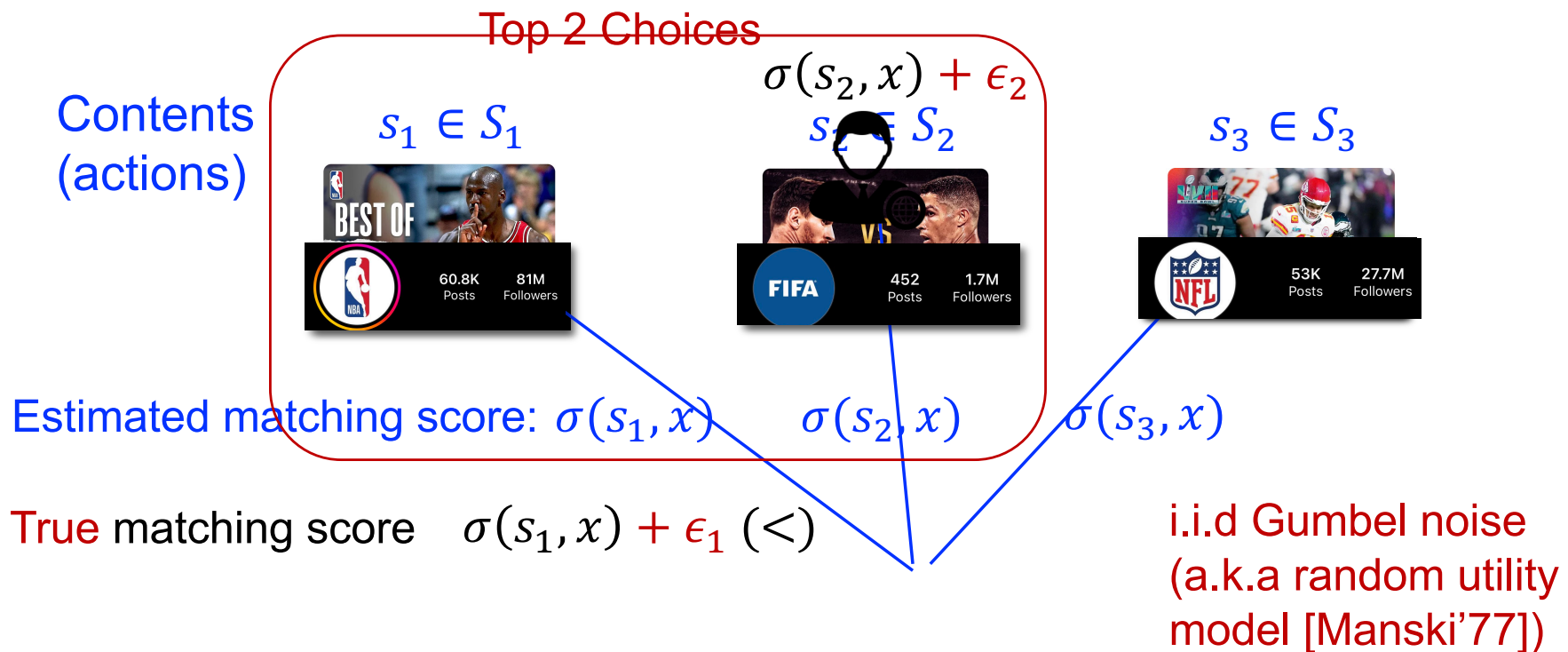
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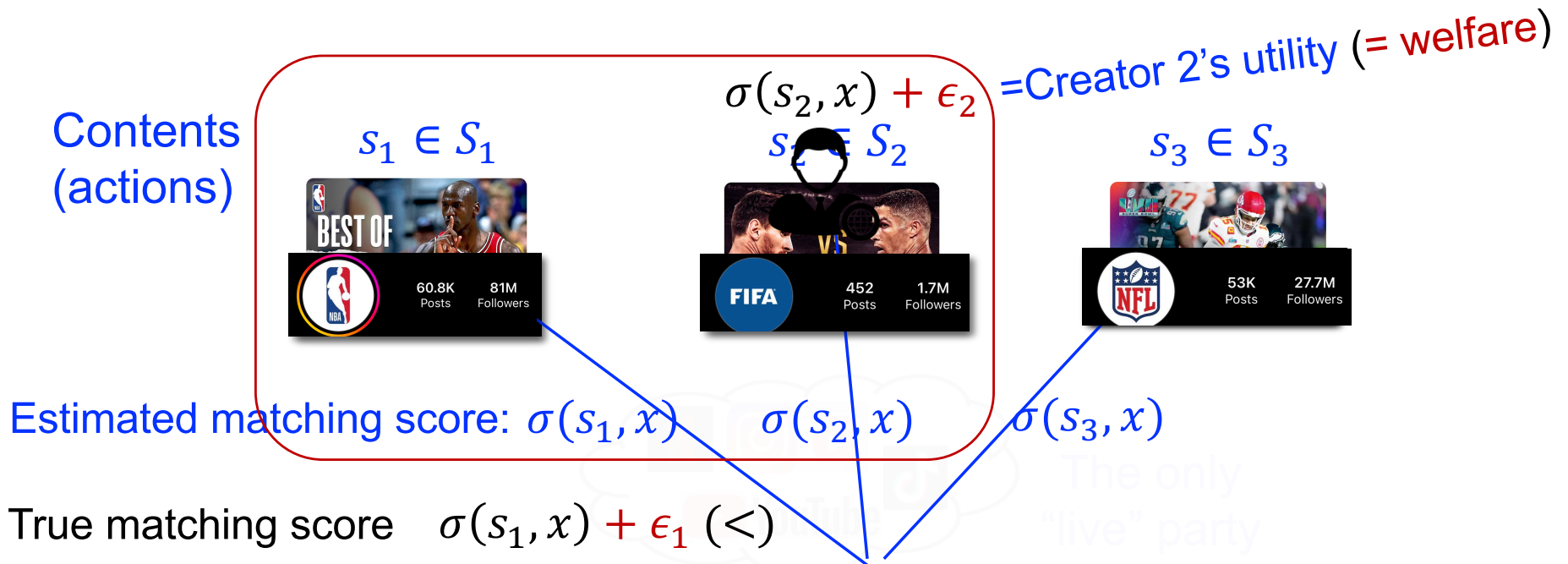
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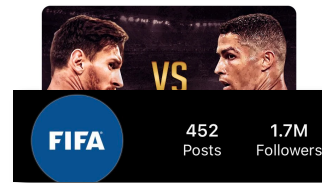
drawn from population/distribution F

Q: do creators' learning dynamics converge to good or bad outcome?

The Competing Content Creation (C3) Game

$$\sigma(s_2, x) + \epsilon_2 = \text{Creator 2's utility (= welfare)}$$

$s_2 \in \mathcal{S}_2$



$$\sigma(s_2, x)$$

How to model each content creator's behavior in the system?

→ Simple – they are just *any* “reasonable” (no-regret) learners who learn to maximize their own users' welfare/happiness

$$\mathbb{E}_{x \sim F} [(\sigma(s_2, x) + \epsilon_2) \cdot \mathbb{I}(x \text{ visits the creator})]$$

Q: do creators' learning dynamics converge to good or bad outcome?

The Competing Content Creation (C3) Game

$$\sigma(s_2, x) + \epsilon_2 = \text{Creator 2's utility (= welfare)}$$

$s_2 \in S_2$

- The goal here is NOT to learn $\sigma(s, x)$ or set S_i 's
- Goal is to study **convergence property** in C3 under (non-stationary) creator learning dynamics, and resultant **system welfare**

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- Goal is to study **convergence property** in C3 under (non-stationary) creator learning dynamics, and resultant **system welfare**
 - We do not directly consider revenue, but RS's revenue is often aligned with total user welfare

→ Simple – they are just *any* “reasonable” (no-regret) learners who learn to maximize their own users' welfare/happiness

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Q: do creators' learning dynamics converge to good or bad outcome?

Theorem [YLNWX, ICML'23]. In any C3 games, if each creator generates contents via *any* no regret learning algorithms, then w.h.p.

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \geq 1 - \frac{1}{1 + (1 + \beta) \log(K)}$$

K = # of recommendation slots
 β^2 = variance of Gumbel noise

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Remark

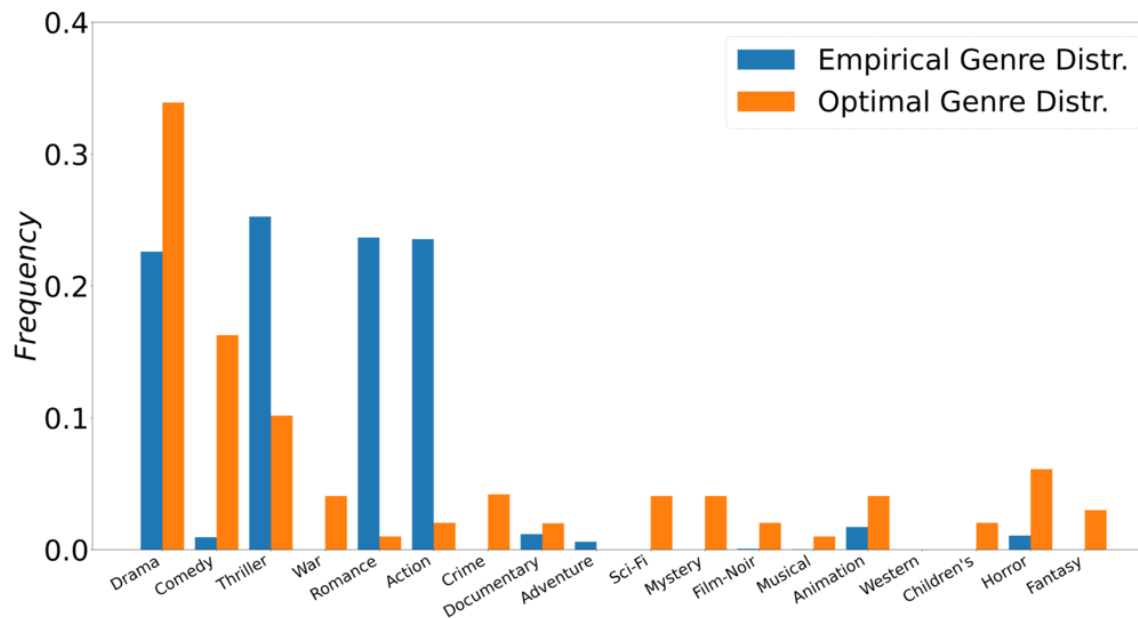
- Also known as the *price of anarchy (PoA)*
 - A very plausible and robust prediction about welfare [Blum et al.'08]
- The bound is an intrinsic property of content competition and user choices
 - Independent of matching score function $\sigma(s, x)$ and #users

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Simulation on MovieLens dataset between **empirical** and **ideal** content distributions



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This bound is (order-wise) tight

Prop 1. There exists C3 games such that is PoA (even for Nash) satisfies

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \leq 1 - \frac{1}{2 + 5\beta \log(K)}$$

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Proof Sketch

- Core insight – C3 is a smooth game [Roughgarden'12]
- Proof turns out to be quite involved
 - Hinges on various analytical properties about the C3 game
 - E.g., total welfare is submodular in the set of contents

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- Proof turns out to be quite involved
 - Hinges on various analytical properties about the C3 game
 - E.g., total welfare is submodular in the set of contents
- **Fun fact:** smoothness technique for C3 yields (order-wise) tight PoA
 - Before this, only 3 classes of games are known to satisfy this (linear congestion game, second price auction and valid utility games)

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Economic insights:

- More recommendation slots (K large), more efficient the system is

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Economic insights:

- More recommendation slots (K large), more efficient the system is
- Setting proper creator incentives matters a lot!

In previous model Creator's utility \sim True user matching score
 $= \sigma(s_2, x) + \epsilon_2$
 \approx user engagement

What if Creator's utility \sim Pr(being matched to user)
 \approx user traffic

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Economic insights:

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Prop 2. Suppose creators' utilities are propositional to **user traffic** in C3 games, then there are C3 games such that

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \leq \frac{1}{2}$$

What if

Creator's utility \sim Pr(being matched to user)
 \approx **user traffic**

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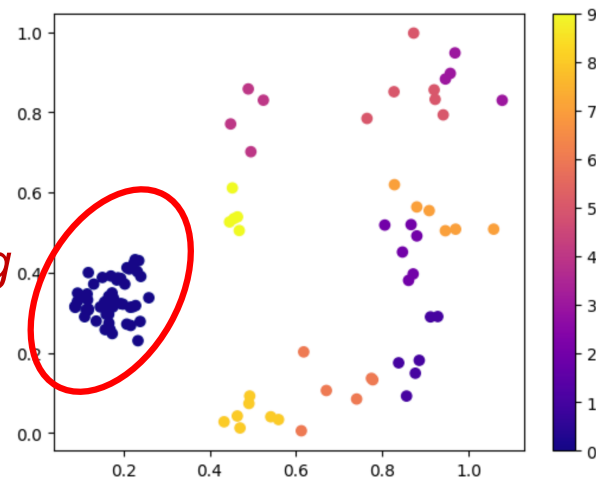
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What situation is worrisome?

Trend-vs-Niche!

A dominating user group



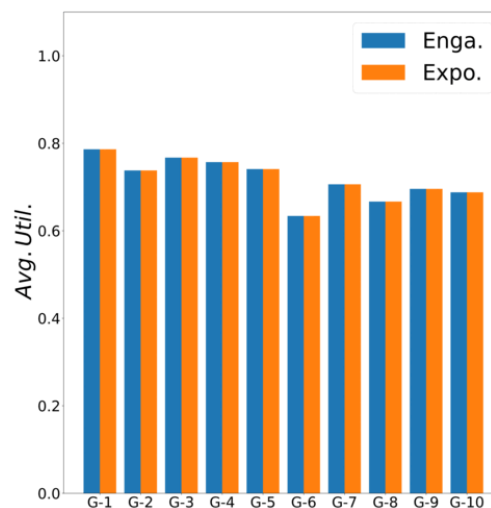
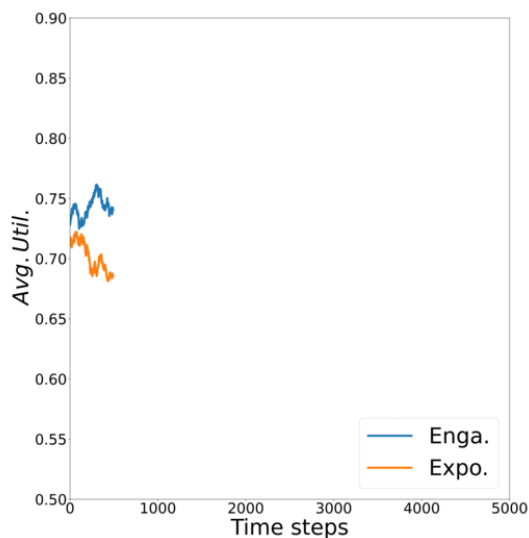
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Economic insights:

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Simulations of no-regret creators on synthetic data

— user engagement
— user traffic

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Economic insights:

- More recommendation slots (K large), more efficient the system is
- Setting proper creator incentives matters a lot!
- Larger β – users are more explorative – increases efficiency
- **In practice, still constant fraction loss since $K \leq 12$**

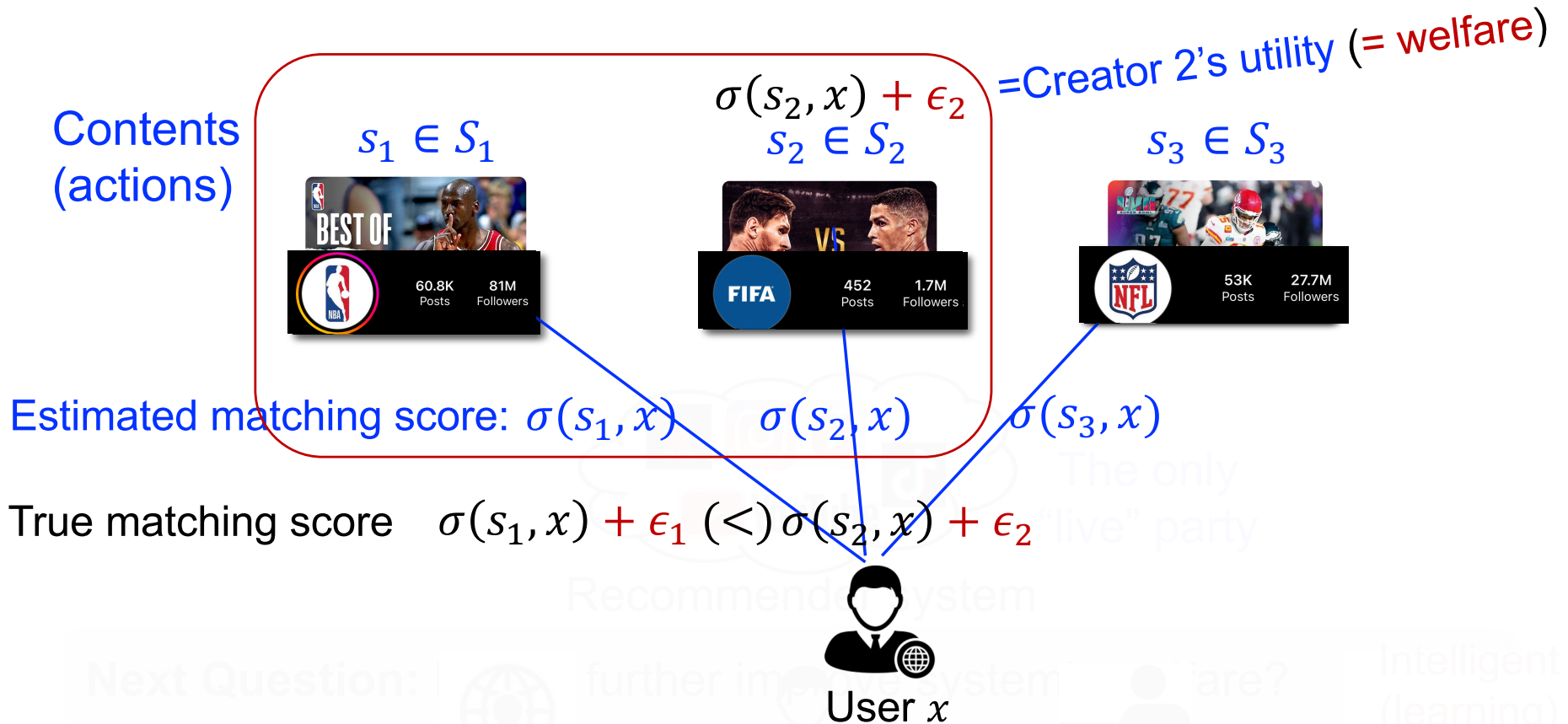
Next Question: how to further improve system's welfare?

Incentive Design for Rewarding Creation

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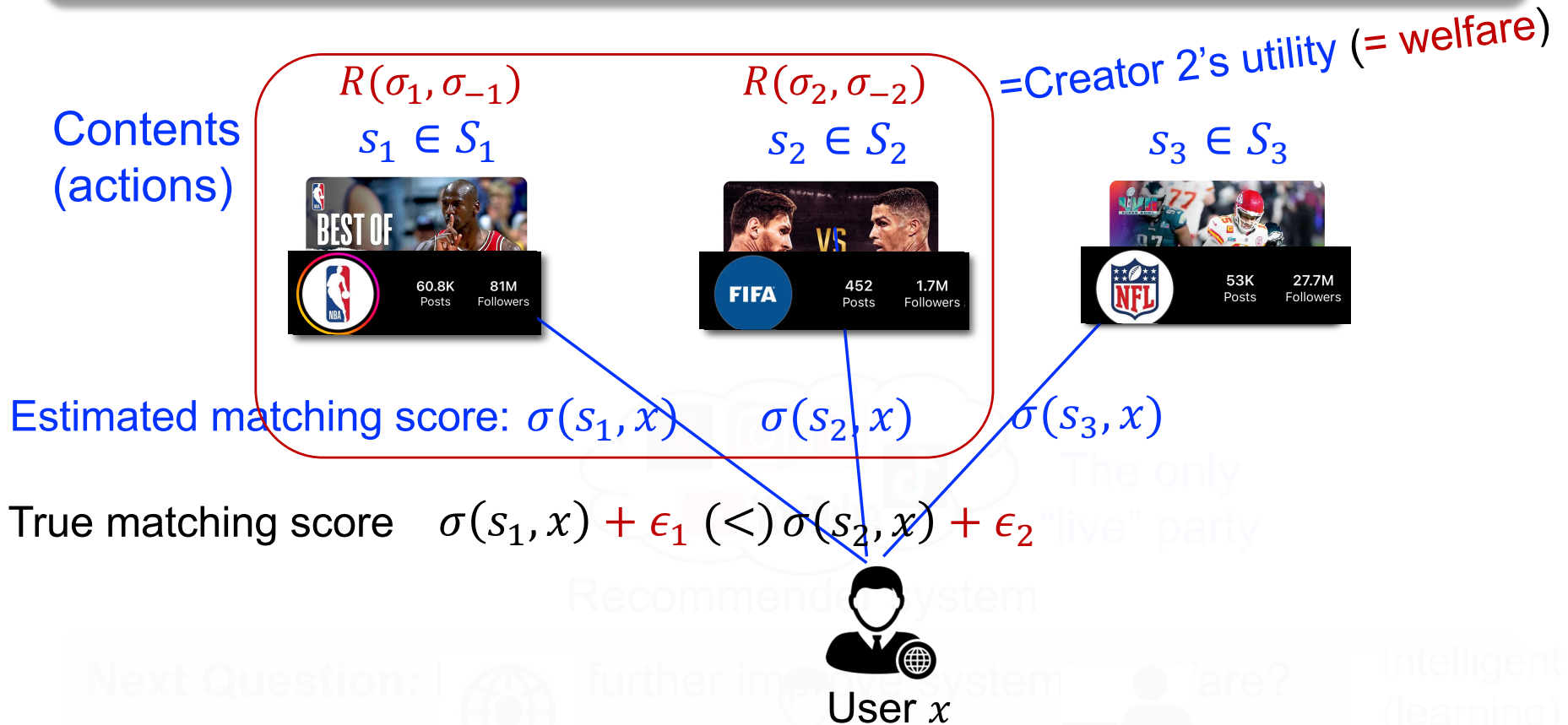
Incentive Design for Rewarding Creation

Previous mechanism's rewards \approx created welfare



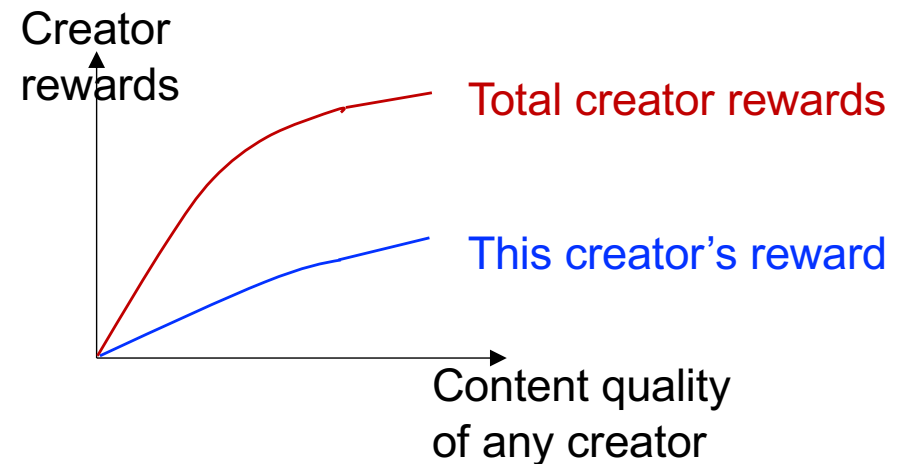
Incentive Design for Rewarding Creation

Q: Can we design/optimize the reward values R to “steer”/incentivize creators’ collective behaviors towards better total welfare?



Why current rewarding mechanism may not be good?

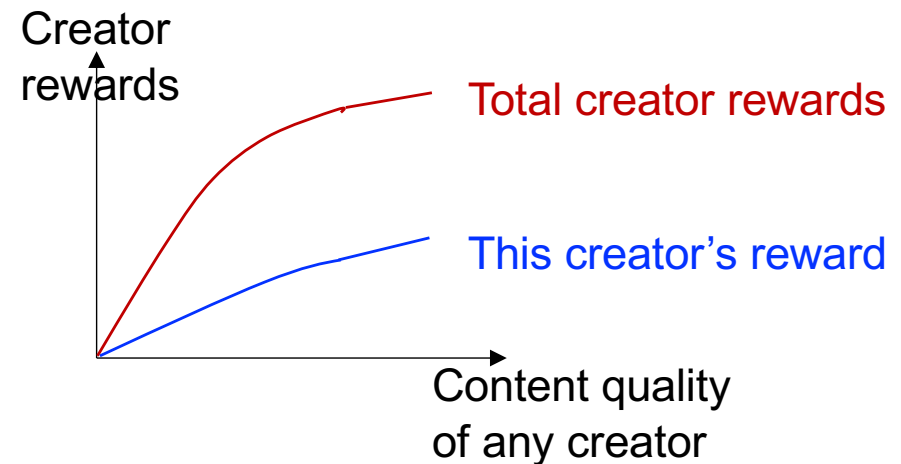
Theorem [Yao et al.'23]. If a rewarding mechanism R are both **individual-monotone** (better contents get more rewards) and **group-monotone**, then it necessarily suffer at least $1/K$ fraction of welfare loss at equilibrium



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- *User engagement and user traffic* do satisfy both; so do many natural rewarding mechanisms in real-world

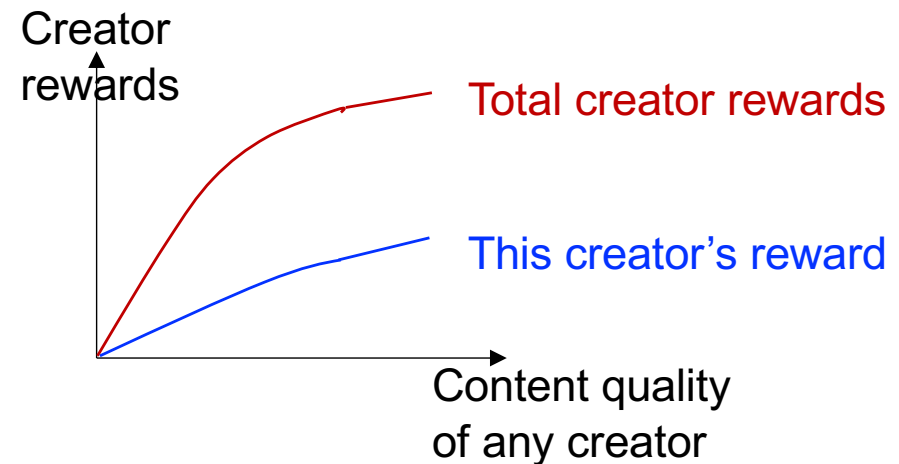


“Rethinking Incentives in Recommender Systems”

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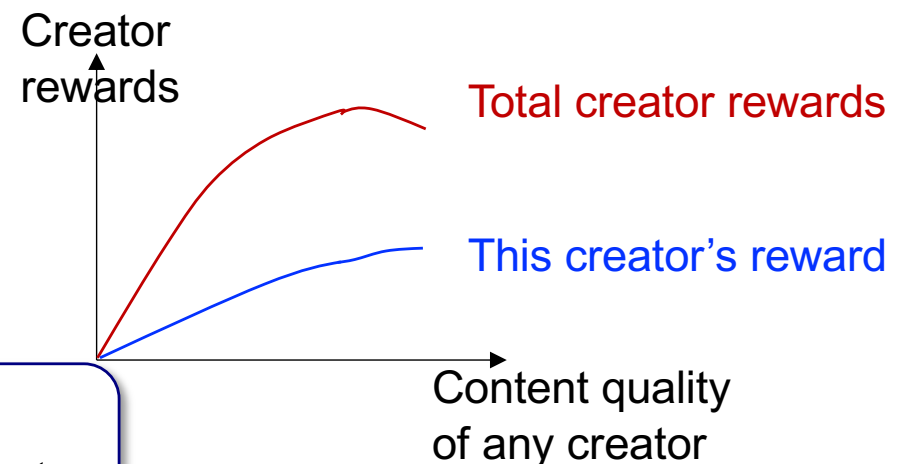


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- *User engagement and user traffic* do satisfy both; so do many natural rewarding mechanisms in real-world
- To overcome this limitation, we **drop group-monotonicity**



Why reasonable?

Group-monotonicity is generally not satisfied in economic markets!

“Rethinking Incentives in Recommender Systems”

Our new mechanism. We designed a new rewarding mechanism that drops group-monotonicity, but provably achieves optimal welfare

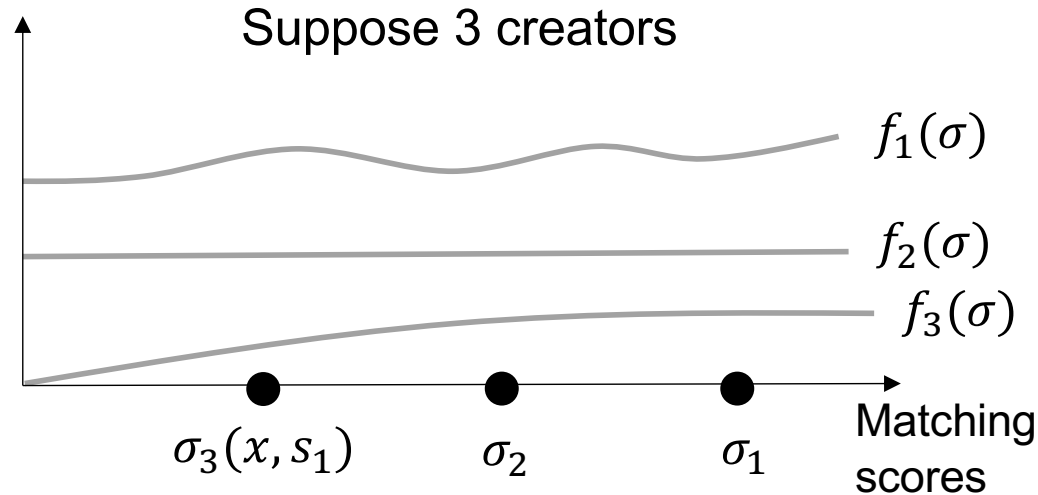
Core idea: reward based on how much you are better than the next

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Core idea: reward based on how much you are better than the next

➤ Mechanism is fully described by functions f_1, f_2, f_3

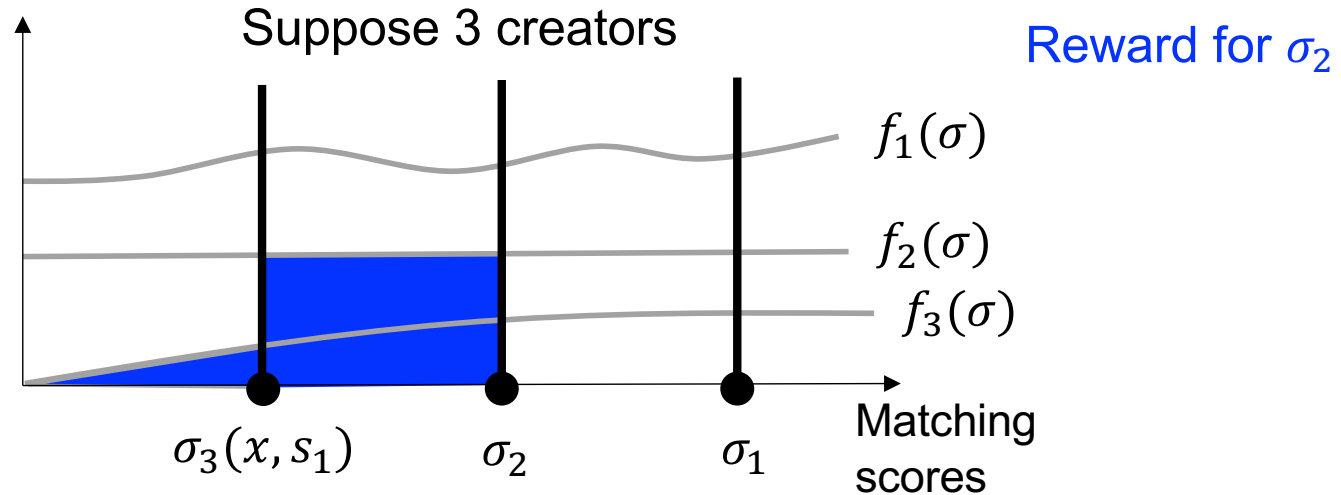


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- Reward = area of ■

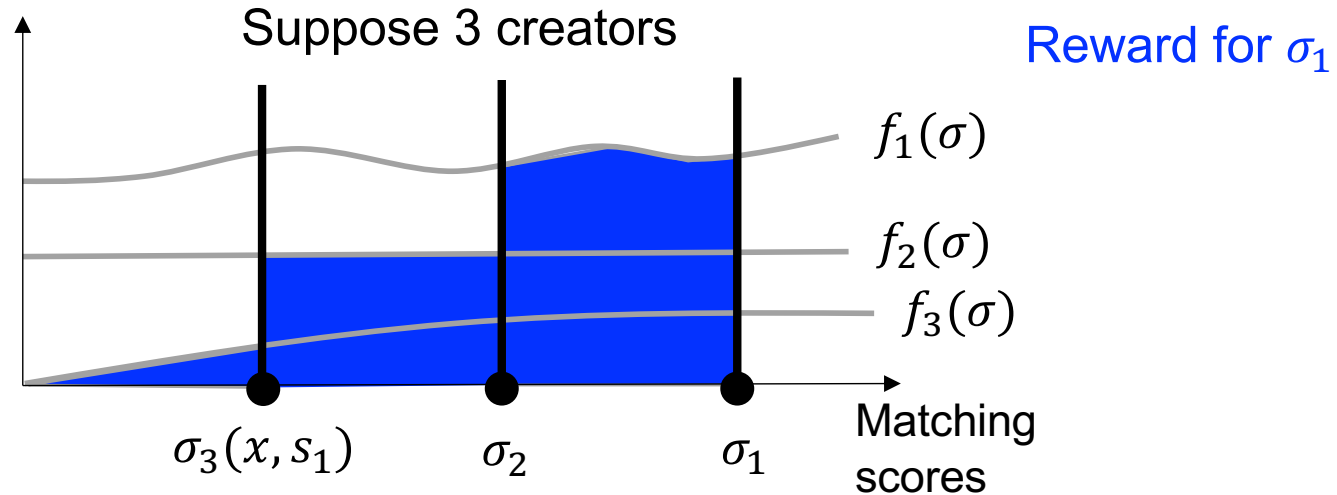


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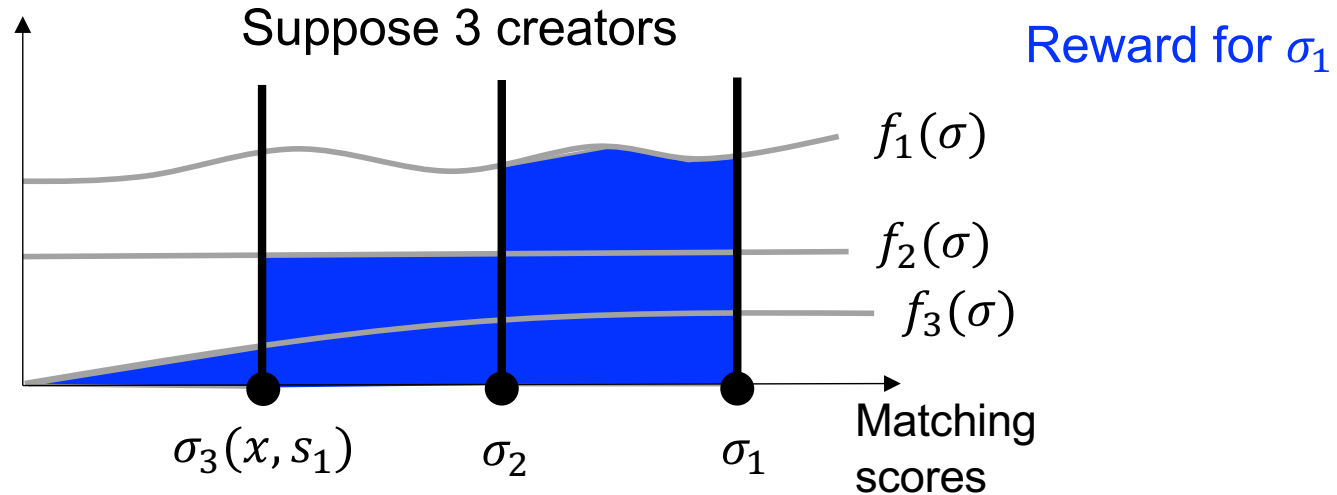
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Advantages

- ✓ σ_1 's reward decreases when σ_2 becomes better (i.e., competition reduces rewards)



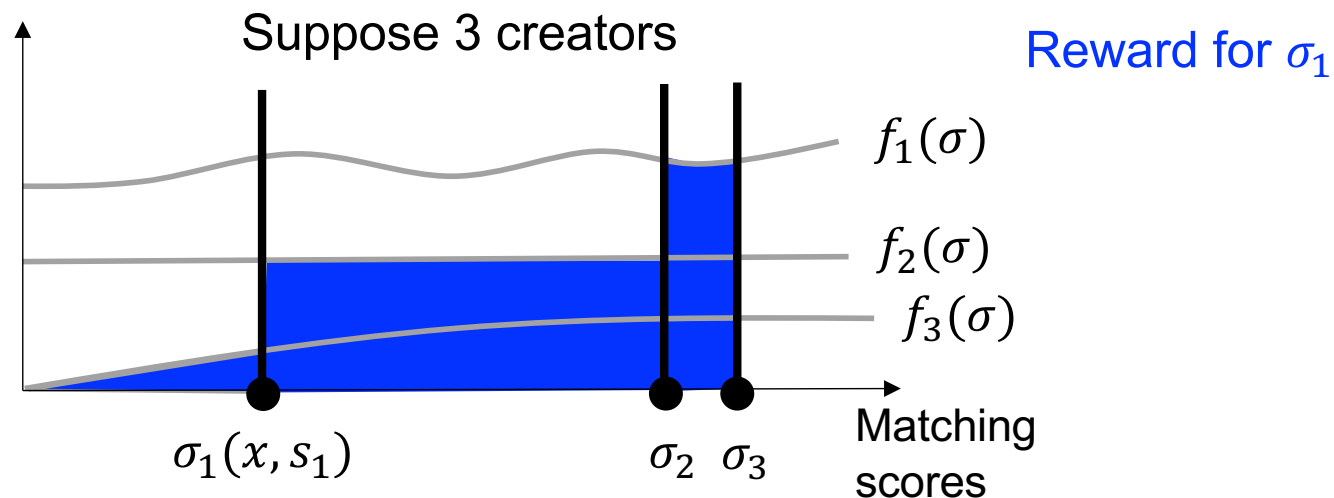
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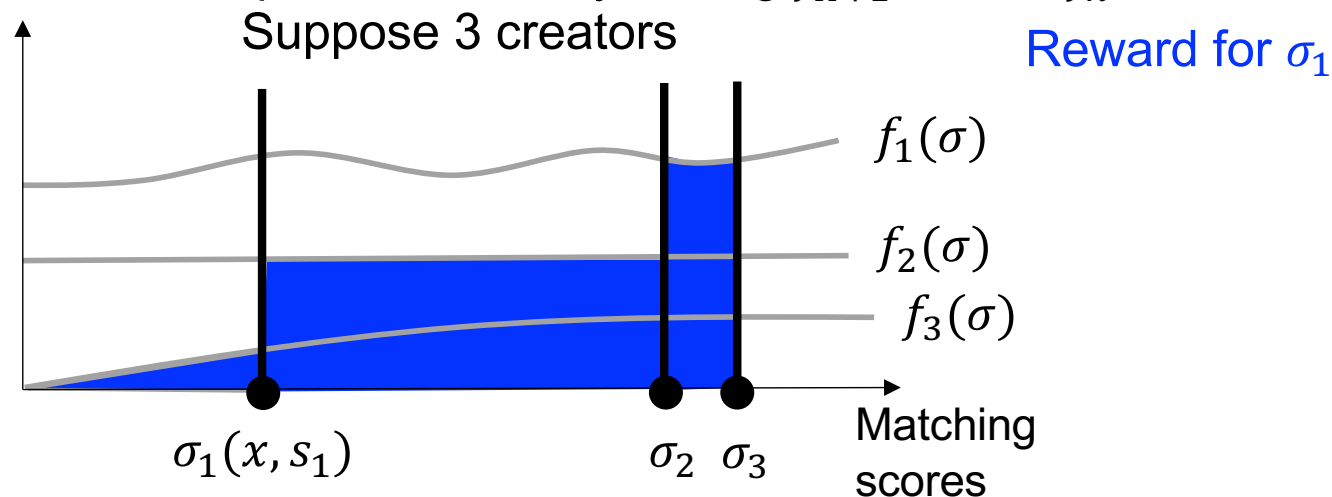
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Advantages

- ✓ σ_1 's reward decreases when σ_2 becomes better (i.e., competition reduces rewards)
- ✓ Naturally handles top- K selection by setting $f_{K+1} = \dots = f_n = 0$



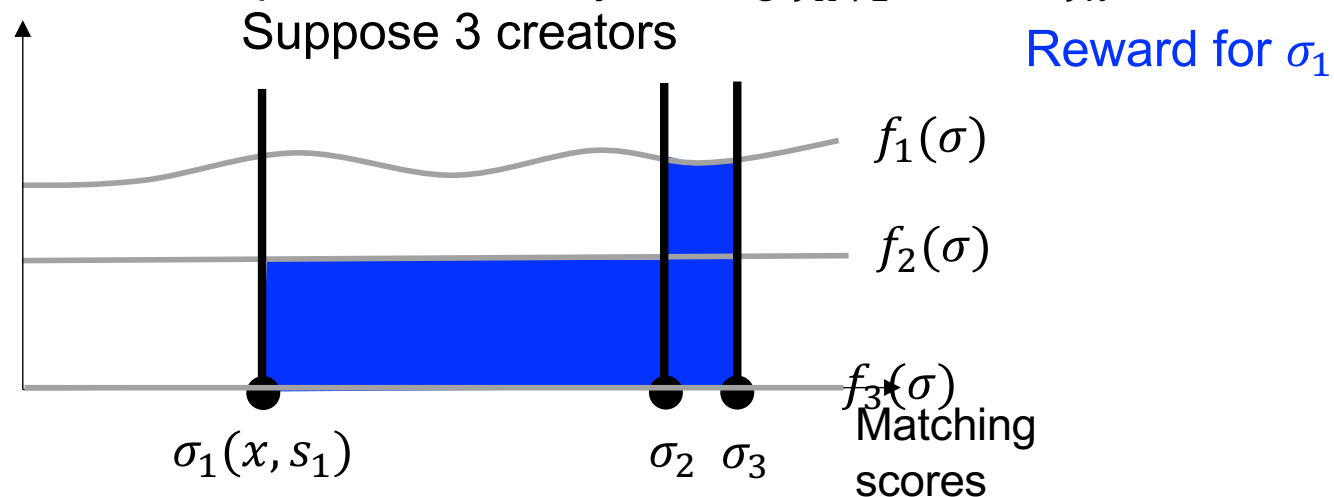
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Core idea: reward based on how much you are better than the next

Advantages

- ✓ σ_1 's reward decreases when σ_2 becomes better (i.e., competition reduces rewards)
- ✓ Naturally handles top- K selection by setting $f_{K+1} = \dots = f_n = 0$



“Rethinking Incentives in Recommender Systems”

Our new mechanism. We designed a new rewarding mechanism that drops group-monotonicity, but provably achieves optimal welfare

- Proof idea: the reward mechanism above induce a potential game among creators, such that potential function = welfare function

“Rethinking Incentives in Recommender Systems”

Our new mechanism. We designed a new rewarding mechanism that drops group-monotonicity, but provably achieves optimal welfare

- Proof idea: the reward mechanism above induce a potential game among creators, such that potential function = welfare function
- Project done in collaboration with researchers at Meta
- Under live experiments on Instagram for >1month now
 - Disclaimer: the deployed algorithm is inspired by, but different from the exact design above

 Meta



Outline

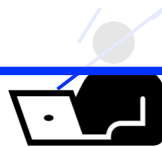


Intelligent
(learning)

Part 1: Interacting with Strategic Creators



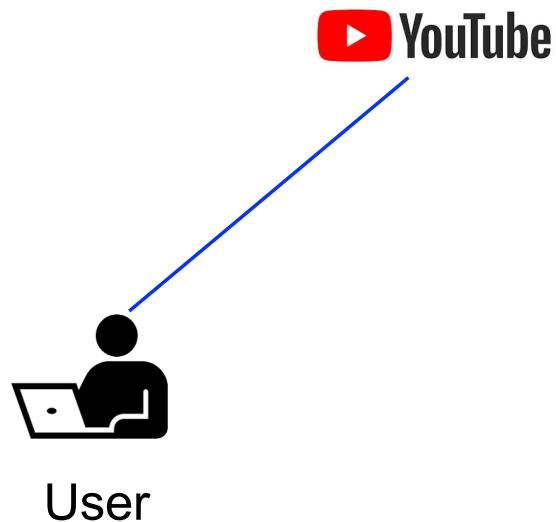
Part 2: Learning from Learning Users



Intelligent
(learning)
users

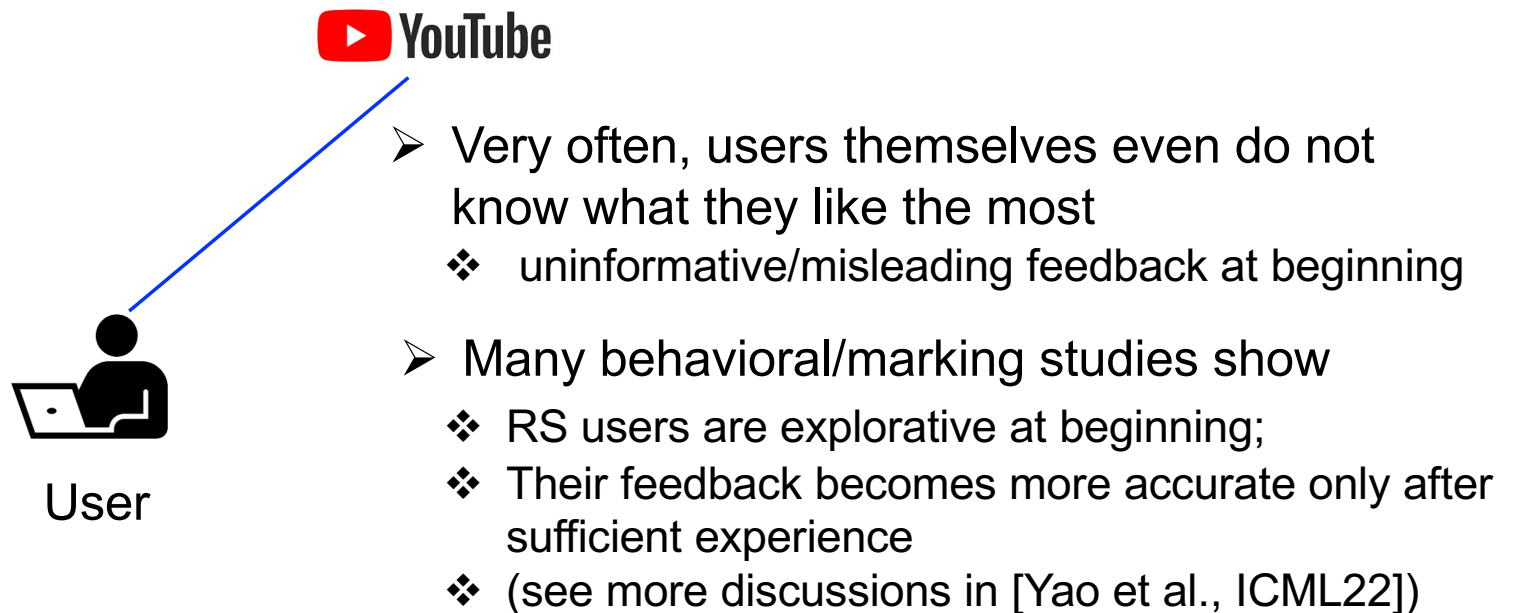
Different Research Challenges

| | Creator side | User side |
|------------------|------------------------------------|----------------------------------|
| Difficult | Incentives, Strategic behaviors | User preferences |
| Easy | Contents' embedding | Incentive (typically aligned) |



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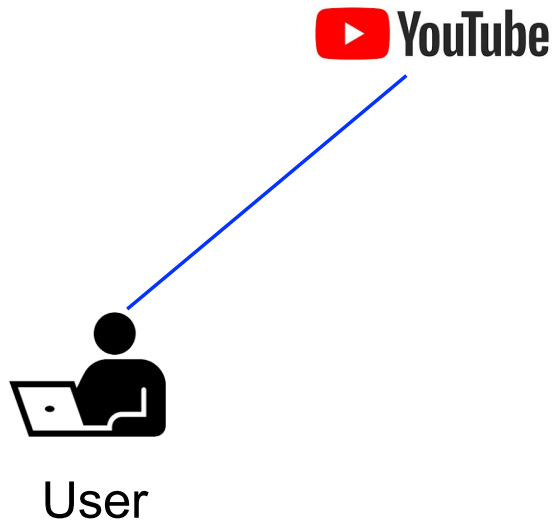
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Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

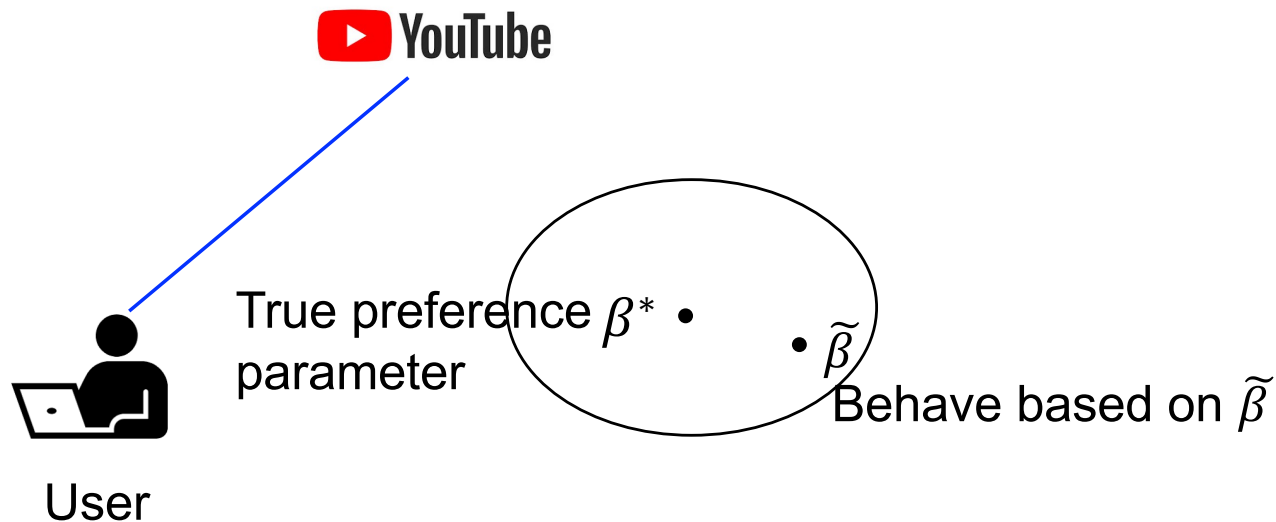
❖ Learning from learning users



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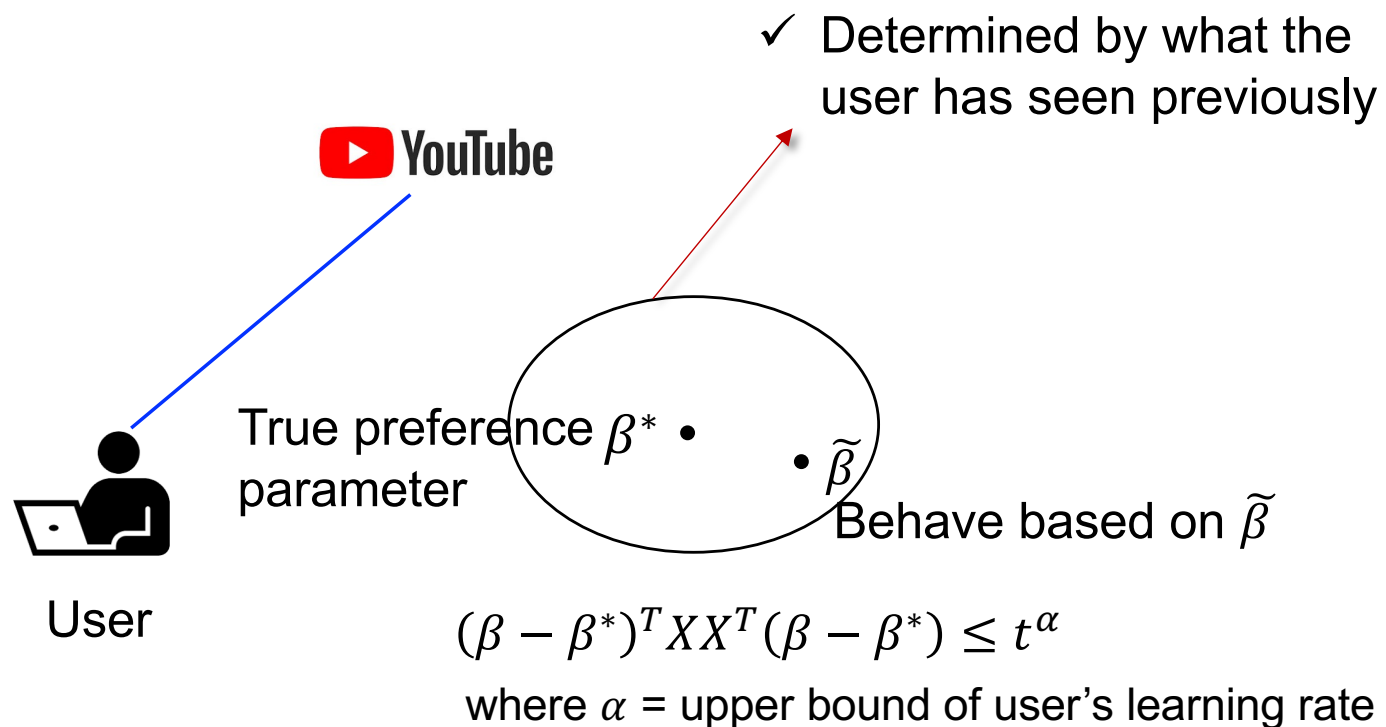
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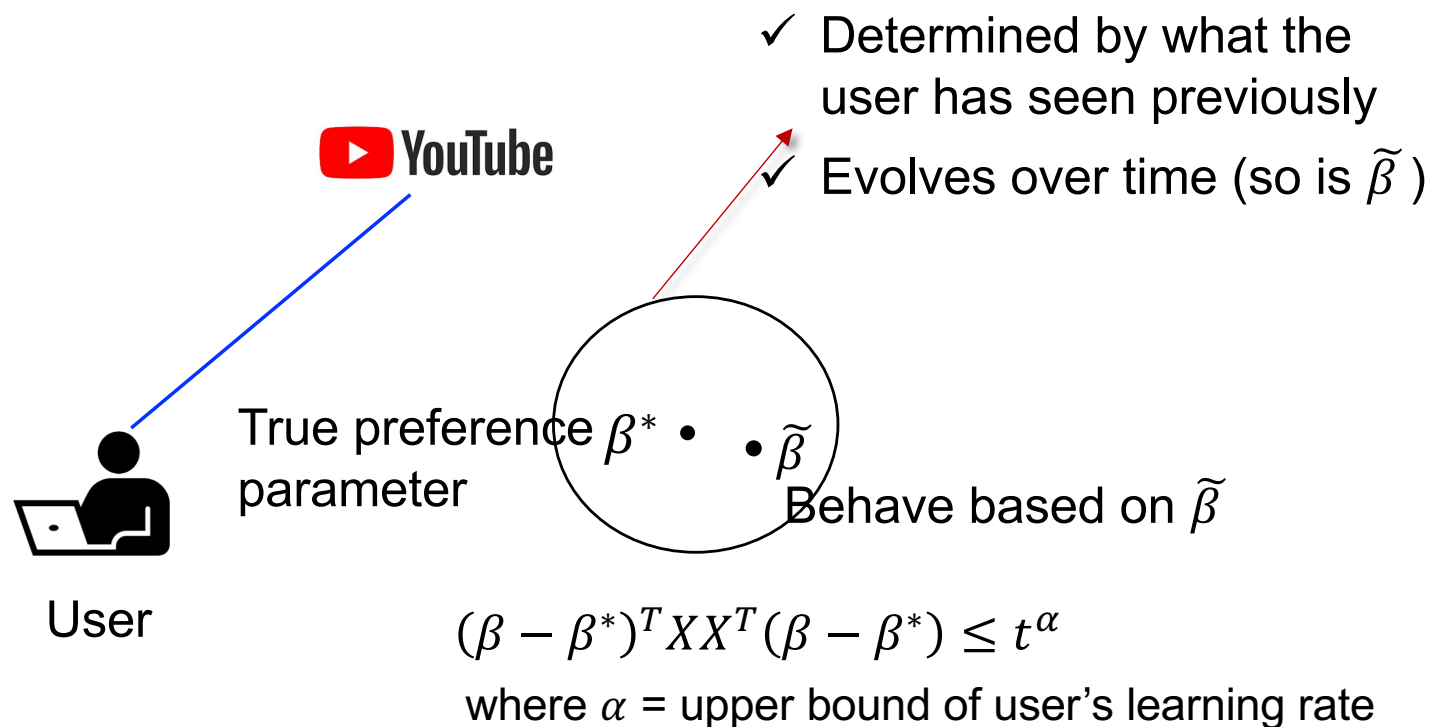
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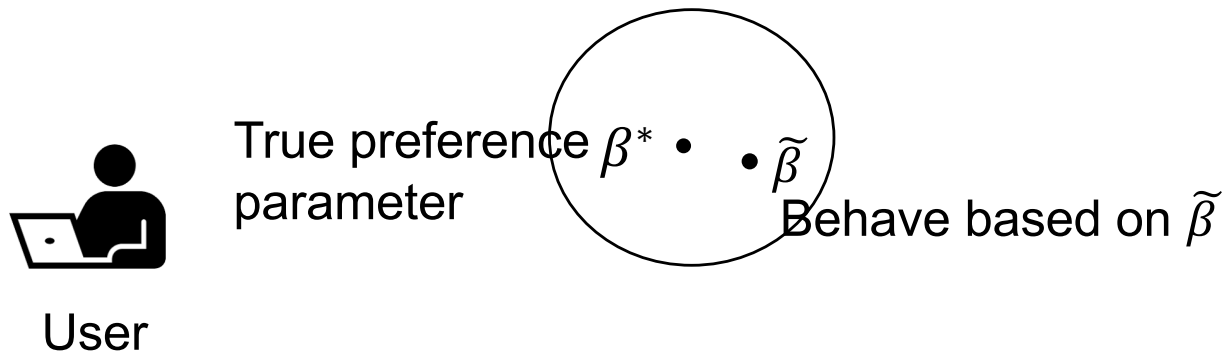
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Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

Can design algorithm to effectively learn from such non-stationary user feedback (driven by user's own learning)



Different Research Challenges

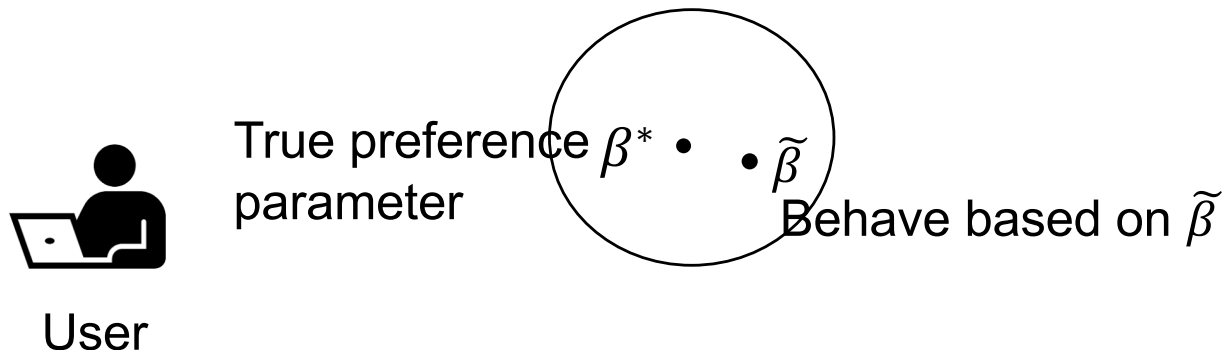
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Core ideas

✓ Cultivate user's own learning at first with more aggressive exploration

⚠ Challenge: tailor exploration time based on user's learning rate α



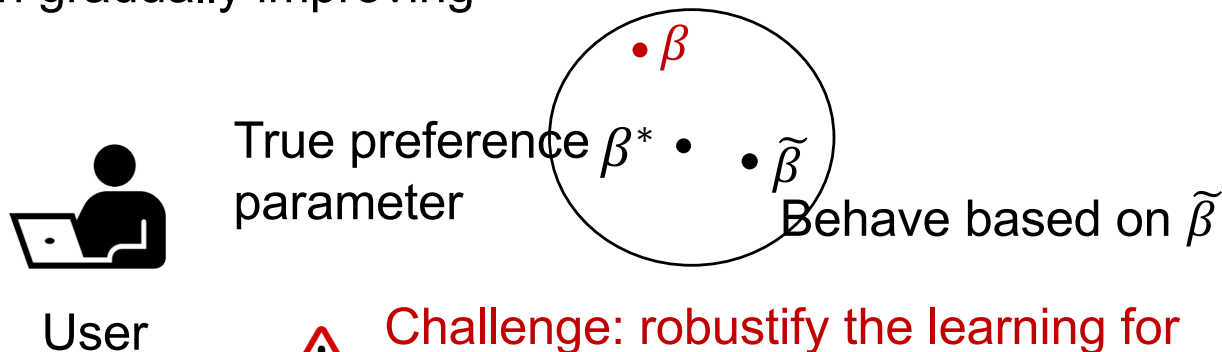
Different Research Challenges

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Core ideas

- ✓ Cultivate user's own learning at first with more aggressive exploration
- ✓ Robustify the use of user's reward feedback, since it is never perfect though gradually improving



Challenge: robustify the learning for arbitrary β in the confidence region

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

Can design algorithm to effectively learn from such non-stationary user feedback (driven by user's own learning)

Overall, it is good news!

Theorem [informal]. There is an algorithm that learns optimal user preferences with regret $O(T^{0.5+\alpha})$ where α is user's own learning rate.

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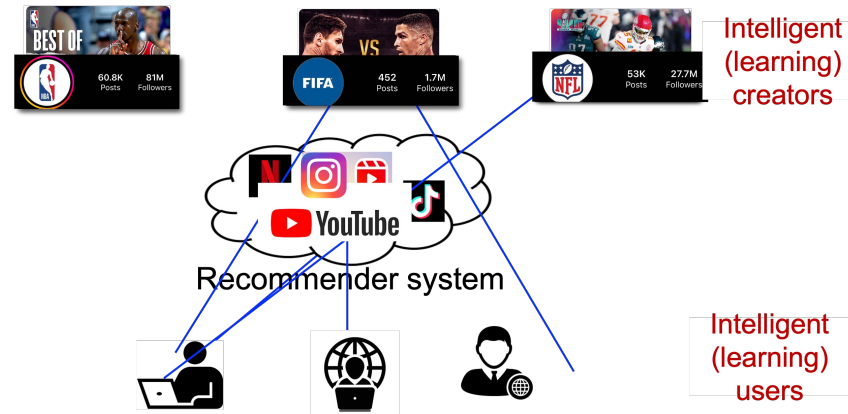
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Overall, it is good news!

Theorem [informal]. There is an algorithm that learns optimal user preferences with regret $O(T^{0.5+\alpha})$ where α is user's own learning rate.

- $\alpha = 0 \rightarrow$ perfect user, in which case we recover optimal regret for standard setups
- Generally, learning efficiency degrades gracefully as user less efficient

Conclusions



- A framework for economic modeling of **contemporary system-creator-user** learning + optimization
- Examined some basic questions during system-creator and system-user interactions
- Many open questions
 - What if three parties are learning contemporarily?
 - What if user preference is contextual as well? (e.g., $\theta(x) = \Theta \cdot x$ where x is a search query)

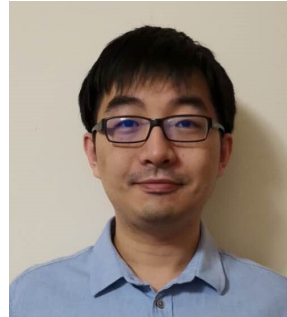
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Hongning wang



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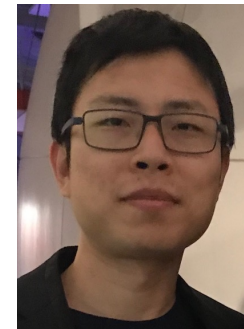
Karthik
Sankararaman



Yiming Liao



Yan Zhu



Qifan Wang

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Fan Yao, Chuanhao Li, Karthik Abinav Sankararaman, Yiming Liao, Yan Zhu, Qifan Wang, Hongning Wang and Haifeng Xu, working paper

And many references therein!

Thank You
Questions?

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